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# THE ELECTRONIC STRUCTURE OF THE $RMn_2Ge_2$ (R = Ca, Y, La, Ba) ANTIFERROMAGNETS

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The electronic structure of the tetragonal RMn<sub>2</sub>Ge<sub>2</sub> (R = Ca, Y, La, Ba) antiferromagnets is presented using the self-consistent Korringa-Kohn-Rostoker method. According to the neutron refinements, two types of collinear antiferromagnetic structure are taken into account: AF<sub>1</sub> for YMn<sub>2</sub>Ge<sub>2</sub> and AF<sub>2</sub> for the other compounds. The calculated magnetic moments on Mn: 2.17  $\mu_B$  (YMn<sub>2</sub>Ge<sub>2</sub>), 2.84  $\mu_B$  (CaMn<sub>2</sub>Ge<sub>2</sub>), 2.95  $\mu_B$  (LaMn<sub>2</sub>Ge<sub>2</sub>), and 3.47  $\mu_B$ (BaMn<sub>2</sub>Ge<sub>2</sub>) remain in good agreement with the neutron data (in  $\mu_B$ ) 2.20, 2.67, 3.05, and 3.66, respectively. As seen on antiferromagnetic density of states, all systems are metallic, however BaMn<sub>2</sub>Ge<sub>2</sub> is found near semimetallic limit. The total energy Korringa-Kohn-Rostoker computations on CaMn<sub>2</sub>Ge<sub>2</sub>, performed in both antiferromagnetic phases, result in preferring of the AF<sub>2</sub> structure.

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# 1. Introduction

The magnetic properties of the well-known ternary RMn<sub>2</sub>Ge<sub>2</sub> compounds [1] with the tetragonal ThCr<sub>2</sub>Si<sub>2</sub>-type structure have attracted renewed interest in recent years. Detailed neutron diffraction investigations of many RMn<sub>2</sub>Ge<sub>2</sub> have revised previously detected ferromagnetic (F) structures (R = La-Nd) [2, 3] and explored the magnetic behavior of new compounds (CaMn<sub>2</sub>Ge<sub>2</sub> and BaMn<sub>2</sub>Ge<sub>2</sub> [4]). In LaMn<sub>2</sub>Ge<sub>2</sub>, antiferromagnetic ordering (AF<sub>2</sub>) occurs below  $T_N \approx 400$  K whereas rather canted magnetic structure than *c*-axis collinear ferromagnetism appears below  $T_C$ , with the antiferromagnetic component markedly larger ( $\mu_{AF} = 2.7 \ \mu_B$ ) than the ferromagnetic one ( $\mu_F = 1.5 \ \mu_B$ ). These results have been later supported by the Mössbauer effect measurements [5]. The three other entitled compounds show purely AF ordering of the Mn magnetic moments. There is a critical distance between Mn atoms in the a-b plane ( $d_{in} = a/\sqrt{2} \approx 2.86$  Å), where the magnetic properties change drastically (mostly due to the AF<sub>1</sub>-AF<sub>2</sub> transition).

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Thus, in YMn<sub>2</sub>Ge<sub>2</sub> ( $d_{in} = 2.82$  Å)  $\mu_{Mn}$  are arranged parallel in the Mn plane and coupled AF between the planes (AF<sub>1</sub>-type) [6], while in CaMn<sub>2</sub>Ge<sub>2</sub> ( $d_{in} = 2.94$  Å) and BaMn<sub>2</sub>Ge<sub>2</sub> ( $d_{in} = 3.14$  Å) the neighboring  $\mu_{Mn}$  are aligned antiparallel both in and between the manganese planes (AF<sub>2</sub>-type) [4]. Ishida et al. [7] have calculated the electronic structure of the "ferromagnetic" LaMn<sub>2</sub>Ge<sub>2</sub> by the Korringa-Kohn-Rostoker (KKR) method. However, the theoretical values of  $\mu_{tot}$ and  $\mu_{Mn}$  have been found rather in disagreement with experimental data available at this time. Furthermore, Kulatov et al. [8] have discussed magnetic ordering of RMn<sub>2</sub>Si<sub>2</sub> and magnetic transition near  $d_{in} \approx 2.86$  Å, using the non-polarized linear muffin-tin orbital (LMTO) results.

The purpose of this paper is to show the electronic structure and magnetism of  $\text{RMn}_2\text{Ge}_2$  using experimentally detected magnetic ordering of  $\mu_{\text{Mn}}$ .

#### 2. Computational details

The spin-polarized calculations on the tetragonal body-centered (bct) RMn<sub>2</sub>Ge<sub>2</sub> compounds are performed by the spin and charge self-consistent KKR method [9, 10] within the local spin density framework (the exchange-correlation potential given by the von Barth-Hedin formula [11]). In the RMn<sub>2</sub>Ge<sub>2</sub> structure (*I4/mmm*) R, Mn, and Ge atoms occupy 2(a) [0,0,0], 4(d) [0,1/2,1/4] and 4(e) [0,0,z] Wyckoff sites, respectively. The crystallographic data measured at T = 2 K [2-4] and muffin-tin radii  $r_{\text{R}} : r_{\text{Mn}} : r_{\text{Ge}} \approx 1.5 : 1 : 1$  (giving  $\sum V_{\text{int}}^i/V_{\text{WS}} \approx$ 67%) are used in the KKR computations. For the final potentials ( $\Delta E_{\text{tot}} \approx 1 \text{ mRy}$ ) the total densities of states (DOS), site-decomposed DOS and *l*-decomposed DOS (with  $l_{\text{max}} = 2$  for R = Ca, Y, Ba and  $l_{\text{max}} = 3$  for R = La) are computed. The relativistic effects are incorporated in calculations of core levels in BaMn<sub>2</sub>Ge<sub>2</sub> and LaMn<sub>2</sub>Ge<sub>2</sub>. Note that in YMn<sub>2</sub>Ge<sub>2</sub> (AF<sub>1</sub>), no more bct symmetry is maintained, then the KKR calculations are performed within the simple tetragonal structure. Integration in the *k*-space is performed using 192 small tetrahedrals and 135 *k*-points in the irreducible part of the Brillouin zone.

### 3. Results and discussion

The main KKR results for RMn<sub>2</sub>Ge<sub>2</sub>, calculated both in F and AF states, are summarised in Table. The theoretical values of  $\mu_{Mn}$  remain in close agreement with the neutron diffraction data, recently measured at T = 2 K [2-4]. The magnetisation (4.22  $\mu_B$ ) as well as the Mn magnetic moments (2.29  $\mu_B$ ) found in the ferromagnetic LaMn<sub>2</sub>Ge<sub>2</sub> are also close to the earlier theoretical values (3.9  $\mu_B$  and 2.1  $\mu_B$ ) [7]. From comparison of the F and AF results one notes that  $\mu_{Mn}$  in the AF<sub>2</sub>-type compounds are rather larger than these computed in the F state (particularly in LaMn<sub>2</sub>Ge<sub>2</sub>), while they are almost the same in YMn<sub>2</sub>Ge<sub>2</sub> (AF<sub>1</sub>-type ordering).

If plotting the theoretical  $\mu_{Mn}$  versus  $d_{in}$  in the RMn<sub>2</sub>Ge<sub>2</sub> antiferromagnets (Fig. 1) we observe that the Mn magnetic moment increases more or less proportionally to  $d_{in}$ , which well corresponds to the phenomenological relations established among  $d_{in}$ ,  $\mu_{Mn}$  and magnetic ordering type [12]. Nevertheless, one should take care using this simple model (Fig. 1), since in real samples when lattice constants increase,  $z_{Ge}$  also changes. A number of the KKR computations on

the RMn<sub>2</sub>X<sub>2</sub> systems, carried out with the use of different a, c and  $z_X$  parameters, lead to conclusion that the  $z_X$  value (like  $d_{in}$ ) has a strong influence on a magnitude of  $\mu_{Mn}$  in RMn<sub>2</sub>X<sub>2</sub>. Moreover, both  $z_X$  and  $d_{in}$  seem crucial in appearing of magnetic properties in RT<sub>2</sub>X<sub>2</sub> (with T  $\neq$  Mn) [13].



Fig. 1. The Mn magnetic moment (in  $\mu_B$ ) versus the Mn-Mn distance ( $d_{in}$ ) in RMn<sub>2</sub>Ge<sub>2</sub>.

#### TABLE

The KKR results in  $RMn_2Ge_2$  (magnetic moments in  $\mu_B$ , DOS in states/Ry/spin).

		$\mathbf{D} = \mathbf{I}_{\mathbf{A}}$	$\mathbf{D} - \mathbf{D}_{\mathbf{n}}$
n = 1	$\mathbf{n} = \mathbf{C}\mathbf{a}$	$\mathbf{n} \equiv \mathbf{L}\mathbf{a}$	$\mathbf{h} = \mathbf{D}\mathbf{a}$
F state			
4.02	4.99	4.22	6.78
2.15	2.59	2.29	3.33
18.79	18.69	20.16	27.55
32.80	51.42	65.52	41.14
AF state			
2.17	2.84	2.95	3.48
2.20	2.67	3.05	3.66
47.51*	10.96	48.99	3.06
	$   \begin{array}{r}     4.02 \\     2.15 \\     18.79 \\     32.80 \\   \end{array} $ $   \begin{array}{r}     2.17 \\     2.20 \\     47.51^* \\   \end{array} $	$\begin{tabular}{ c c c c c } \hline $F$ state \\ \hline $4.02$ & $4.99$ \\ \hline $2.15$ & $2.59$ \\ \hline $18.79$ & $18.69$ \\ \hline $32.80$ & $51.42$ \\ \hline $AF$ state \\ \hline $2.17$ & $2.84$ \\ \hline $2.20$ & $2.67$ \\ \hline $47.51^*$ & $10.96$ \\ \hline \end{tabular}$	$\begin{tabular}{ c c c c c c } \hline $F$ state \\ \hline $F$ state \\ \hline $4.02$ & $4.99$ & $4.22$ \\ \hline $2.15$ & $2.59$ & $2.29$ \\ \hline $18.79$ & $18.69$ & $20.16$ \\ \hline $32.80$ & $51.42$ & $65.52$ \\ \hline $AF$ state \\ \hline $2.17$ & $2.84$ & $2.95$ \\ \hline $2.20$ & $2.67$ & $3.05$ \\ \hline $47.51^*$ & $10.96$ & $48.99$ \\ \hline \end{tabular}$

\*per two formula units

The DOS of YMn<sub>2</sub>Ge<sub>2</sub> (AF<sub>1</sub>) (Fig. 2) consists of two broad peaks coming mostly from the Mn sites. Unlikely, the DOS of CaMn<sub>2</sub>Ge<sub>2</sub>, LaMn<sub>2</sub>Ge<sub>2</sub>, and BaMn<sub>2</sub>Ge<sub>2</sub> (AF<sub>2</sub>) presents complex structure with few narrow *d*-like peaks arising also on Mn atoms (note that the highest *d*-like peaks are localized well below  $E_{\rm F}$  in contrast to *d*-DOS in YMn<sub>2</sub>Ge<sub>2</sub>). The conduction band in RMn<sub>2</sub>Ge<sub>2</sub> is formed mostly by *d*-states on Mn and R with some admixture of *p*-states on Ge.



Fig. 2. The total DOS in the RMn<sub>2</sub>Ge<sub>2</sub> antiferromagnets: (a) YMn<sub>2</sub>Ge<sub>2</sub>, (b) CaMn<sub>2</sub>Ge<sub>2</sub>, (c) LaMn<sub>2</sub>Ge<sub>2</sub>, (d) BaMn<sub>2</sub>Ge<sub>2</sub>.

The s-states (not plotted in Fig. 2) form two separate bands and are located 0.13-0.15 Ry below the conduction band bottom. When passing from R = Y to R = Ba (increasing  $d_{in}$ ), less overlapping of d-like wave functions occurs, giving rise to narrow bands. Consequently, Mn atoms keeps successively larger magnetic moment reaching the 3.48  $\mu_{\rm B}$  value (3.66  $\mu_{\rm B}$  from experiment) in BaMn<sub>2</sub>Ge<sub>2</sub>. Interestingly, from the KKR calculations this compound is found near the semimetallic limit (Fig. 2). The  $E(\mathbf{k})$  computations (not shown) result in two strongly dispersive bands crossing the Fermi level, while an energy gap occurs along most of k-vector directions. As CaMn<sub>2</sub>Ge<sub>2</sub> and BaMn<sub>2</sub>Ge<sub>2</sub> have the same number of valence electrons, the low DOS at  $E_{\rm F}$  is also detected in CaMn<sub>2</sub>Ge<sub>2</sub>. In LaMn<sub>2</sub>Ge<sub>2</sub>  $E_{\rm F}$  is shifted into the DOS peak due to one more electron. To investigate a reason for the changing of the AF-type structure, near  $d_{\rm in} \approx 2.86$  Å the total energy KKR computations are done on  $CaMn_2Ge_2$  applying  $AF_1$  and  $AF_2$ . Indeed,  $E_{tot}$  has a slightly lower value when using the  $AF_2$  structure. But the similar comparison in  $YMn_2Ge_2$  does not give reliable preference for  $AF_1$ . Then, more detailed analysis  $E_{\text{tot}} = f(a, c, z_{\text{Ge}})$  should be undertaken to clarify this point.

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