

# Nascent Rotational Distribution of $\text{CO}_2(00^0_0, J)$ States from Collisions with Highly Vibrationally Excited $\text{Na}_2$

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Received: 10.10.2023 & Accepted: 29.02.2024

Doi: [10.12693/APhysPolA.145.347](https://doi.org/10.12693/APhysPolA.145.347)

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In this work, the high vibrational states of  $\text{Na}_2$  were excited via stimulated emission pumping. The full-state resolution distribution of molecular scattering of  $\text{CO}_2(00^0_0, J)$ , resulting from collisions with excited  $\text{Na}_2 X^1\Sigma_g^+$  ( $v'' = 33$  and  $45$ ), was also investigated. In particular, the scattered  $\text{CO}_2(00^0_0, J = 2-80)$  molecules were found to possess a biexponential rotational distribution. The low- and high-energy distributions were derived by fitting the data by means of a biexponential model. The cold distribution accounted for 80% of the total scattering and was caused by elastic or weakly inelastic collisions. Such collisions might have caused very small rotational excitations in  $\text{CO}_2$ . The hot distribution involved substantial changes in the rotational energy of  $\text{CO}_2$  and accounted for 20% of the total amount of collisions. The influence of the donor energy on the rotational distribution was shown to be very large; however, for the two types of donor energies, the branches associated with inelastic and elastic collision rates were the same. The nascent translational energy curves for scattered  $\text{CO}_2(00^0_0, J = 56-80)$  were measured via high-resolution transient overtone fluorescence. For every 25% enhancement in donor vibrational energy, the product translational energy of an individual  $J$ -state increased by 60%. Additionally, the measured collision rates were found to be weakly dependent on the donor energy.

topics: spectroscopy measurement, energy transfer, stimulated emission pumping, excited  $\text{Na}_2$

## 1. Introduction

The scientific understanding of the excited state structure of atoms and molecules not only provides a detailed and reliable experimental basis for theorists but also plays a key role in promoting the development of quantum chemistry, chemical reaction dynamics, and other related disciplines. Thus, a suitable understanding of the molecular energy transfer processes is urgently required in many science and technology fields, including laser chemistry [1], biochemistry [2], applied physics [3], plasma physics [4], aviation technology, and even astronomy [5].

Collisions between highly vibrationally excited molecules (when the internal energy approaches the dissociation limit) and thermal bath molecules play an important role in the breakdown or rearrangement of molecules. The competition between the collisional energy transfer and the reaction determines the chemical reaction kinetics as a whole, as well as the dynamics, thereby affecting many associated atmospheric reactions [6–8] and combustion processes [9].

Numerous spectroscopic approaches relying on ultraviolet (UV) absorption [10], infrared (IR) fluorescence [11], overtone absorption [12], ultrafast transient absorption [13], and optical-optical double resonance [14] have been used to measure the high-energy collisional inactivation of molecules. In particular, the full-state resolved distribution of the nascent energy absorption in hot-bath molecules was analyzed by Mullin's group [15–17] using state-resolved transient spectroscopy. It has been shown that the energy transfer between  $\text{CO}_2$  and pyrazine (with  $E = 32700$  and  $37900 \text{ cm}^{-1}$ ) mainly occurs through a vibration-to-rotation/translation (V-RT) channel. The nascent translational energy produced by the collision is very sensitive to the pyrazine energy. For example, a 16% increase in the pyrazine vibrational energy leads to a 50% increase in the recoil energy of the scattered molecules.

According to the biexponential rotational distribution of scattered  $\text{CO}_2$  molecules, the majority of the collisions are weakly inelastic collisions (77%), and the rest are strongly inelastic collisions (23%). Compared with weak collisions, the distribution of strong collisions is sensitive to the changes in the donor  $E$ . Using stimulated Raman pumping to ex-

cite H<sub>2</sub> ( $v = 1$ ), Shen’s group [18] showed that high-energy donor molecules release more translational energy to the bath. They found that the translational energy increased by 120% when the donor energy was increased by 13%, suggesting that the nascent translational energy of LiH ( $0, J$ ) is sensitive to the H<sub>2</sub> energy. The results also showed that the overall appearance and depletion rate of H<sub>2</sub> at the two different energies were similar, demonstrating that the collision rate constant does not vary with the donor energy. Cui and colleagues [19] found that CO<sub>2</sub> is an efficient relaxation partner for the high vibrational states of KH. They used overtone pumping to excite KH to  $v = 14$ – $21$  and collide with CO<sub>2</sub>, proving that when the internal energy of KH is increased by a factor of 1.27, the average rotational energy of CO<sub>2</sub> increases by a factor of nearly 1.35. The rate coefficient  $k_{v''}(\text{CO}_2)$  depends strongly on the vibrational quantum number of KH, and the mean translational energy of scattered CO<sub>2</sub> molecules increases roughly linearly with the change in the  $J$  state of CO<sub>2</sub>. In the present study, the collisional energy transfer of highly vibrationally excited Na<sub>2</sub> was experimentally measured in a CO<sub>2</sub> bath. A pump–probe technique was employed to obtain highly vibrationally excited Na<sub>2</sub> in its electronic ground state excited to rovibrational states  $X^1\Sigma_g^+(v'' = 33, J'' = 11)$  and  $X^1\Sigma_g^+(v'' = 45, J'' = 11)$  [20], and laser-induced fluorescence (LIF) was used to determine the vibrational states of the system under consideration.

## 2. Experimental methods

Under single-collision conditions, the rotational states of CO<sub>2</sub>(00<sup>0</sup>0) were excited by high overtones and detected using LIF. Despite the fact that the CO<sub>2</sub>(00<sup>0</sup>0,  $J$ ) states were not detected via transient absorption, they could be identified through the following overtone excitation via LIF. The high resolution of the laser allowed us to measure the population of the individual rotational states in the scattered CO<sub>2</sub>(00<sup>0</sup>0) molecules. The rate measurements were conducted for both depletion and appearance of the population in the individual CO<sub>2</sub>(00<sup>0</sup>0,  $J$ ) states.

A schematic of the experimental setup used in this work is shown in Fig. 1. The reaction cell consists of a five-armed crossed heat-pipe oven, in which four arms form a planar cross, while the perpendicular fifth arm, which contains the Na reservoir, is sealed at the base of the intersection of the four arms. The cell is connected to a vacuum instrument through a gas-supplying system that fills the pool with gas at different pressures under vacuum. During the experiment, the Na metal was heated in the bottom reservoir to a temperature between 450 and 900 K. The temperature of the cell was monitored by means of an intrusive thermocouple in

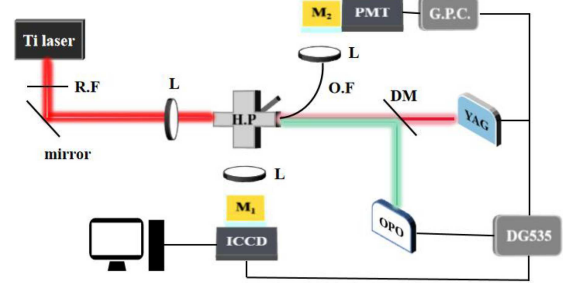


Fig. 1. Experimental setup: H.P — heat pipe oven; OPO — optical parametric oscillator; M — monochromator; PMT — photomultiplier; G.P.C — gated photon counter; DM — dichroic mirror; L — lens; DG535 — pulse delay box; R.F — removable filter; O.F — optical fiber.

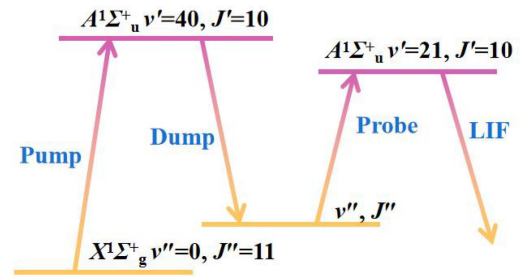


Fig. 2. Energy diagram of the pump–dump and probe scheme.

the vicinity of the collision regime. The CO<sub>2</sub> pressure in the cell was 15 mTorr. The cell was filled with CO<sub>2</sub> gas, which served both as a collision partner for the excited Na<sub>2</sub> molecules and as a buffer gas, preventing Na condensation on the cell windows.

Figure 2 depicts the correlated energy level diagram. The highly vibrationally excited Na<sub>2</sub> molecules  $X^1\Sigma_g^+(v''=33, J''=11)$  and  $X^1\Sigma_g^+(v''=45, J''=11)$  were realized via stimulated emission pumping, and the excited Na<sub>2</sub> states were then probed via LIF. While a YAG laser pulse of 532 nm was used to pump the Na<sub>2</sub> molecules from the  $X^1\Sigma_g^+(v''=0, J''=11)$  state to the  $A^1\Sigma_u^+(v' = 40, J' = 10)$  state [20], an OPO served as a dump laser (with wavelengths of 698 and 763 nm) to ensure that the Na<sub>2</sub>  $A^1\Sigma_u^+(v' = 40, J' = 10)$  state was pumped back to the highly vibrationally excited Na<sub>2</sub>  $X^1\Sigma_g^+(v'' = 33, J'' = 11)$  and  $X^1\Sigma_g^+(v''=45, J''=11)$  states. A continuous-wave (CW) Ti:sapphire (Ti:Sa) laser was employed to probe either the vibrational state or the collisionally populated states of the prepared molecules.

Na<sub>2</sub>  $X^1\Sigma_g^+(v''=33, J''=11)$  and  $X^1\Sigma_g^+(v''=45, J''=11)$  states were excited to the  $A^1\Sigma_u^+(v'=21, J'=10)$  state using 799.7 and 886.3 nm Ti:Sa lasers, respectively. The  $A^1\Sigma_u^+(v'=21, J'=10)$  state of Na<sub>2</sub>

relaxed to the  $X^1\Sigma_g^+(v'' = 0-4)$  state, and LIF was detected using intensified charge-coupled device (ICCD) in the direction perpendicular to the laser propagation direction.

Figure 3 shows a segment of the LIF spectrum of the  $A(v' = 21, J' = 10) \leftarrow X(v'' = 33, J'' = 11)$  band of  $\text{Na}_2$ , revealing that  $J'' = 11$  of  $v'' = 33$  of ground state  $\text{Na}_2$  were prepared. The assignment of the spectrum could be easily performed since the molecular constants of  $\text{Na}_2$  are known for both the upper and lower states. According to Fig. 3, the  $v'' = 33$  state was excited by stimulated emission pumping (SEP).

### 3. Results and discussion

#### 3.1. Density measurements of $\text{Na}_2(v'', J'')$ states

The power of the Ti:Sa laser was kept as small as  $0.1 \mu\text{W}$  using neutral-density filters, and the beam diameter at the center of the cell was adjusted to 1 mm by means of a lens with a focal length of 1 meter and an aperture. The density of the  $\text{Na}_2(v'', J'')$  states was measured by inducing the  $X^1\Sigma_g^+(v'', J'') \rightarrow A^1\Sigma_u^+(v', J')$  transition with the Ti:Sa laser and monitoring its spread. The transmitted intensity  $I_v(L)$  of the laser beam with frequency  $\nu$  after passing through the vapor of length  $L$  was calculated as follows [21]:

$$\frac{\Delta I}{I_v(0)} = 1 - \exp(-k_{\nu', J' \leftarrow \nu'', J''}(\nu) L), \quad (1)$$

where  $\Delta I = I_v(0) - I_v(L)$ ;  $I_v(0)$  is the incident intensity; and  $k_{\nu', J' \leftarrow \nu'', J''}(\nu)$  is the absorption coefficient as a function of frequency. The number density of the  $\text{Na}_2(v'', J'')$  states is related to the integral of the  $k_{\nu', J' \leftarrow \nu'', J''}(\nu)$  function as [21]

$$\int d\nu k_{\nu', J' \leftarrow \nu'', J''}(\nu) = \frac{(\lambda_{\nu', J' \leftarrow \nu'', J''})^2}{8\pi} \frac{g_{J'}}{g_{J''}} [\text{Na}_2(v'', J'')] \Gamma_{\nu', J' \rightarrow \nu'', J''}, \quad (2)$$

where  $g_{J'}$  and  $g_{J''}$  are the degrees of degradation of the  $J'$  and  $J''$  states, respectively;  $\Gamma_{\nu', J' \rightarrow \nu'', J''}$  is the natural radiation rate during the transition, and  $\lambda_{\nu', J' \leftarrow \nu'', J''}$  is the wavelength of the transition.

Figure 4 depicts the time-resolved fluorescence semilogarithmic plot of the  $A^1\Sigma_u^+(v' = 40, J' = 10) \rightarrow X^1\Sigma_g^+(v'' = 45, J'' = 11)$  transformation underwent by  $\text{Na}_2$  upon the excitation of the  $A(40, 10)$  state by the YAG laser. In the experiment, the relationship between  $\ln(\text{signal})$  and  $t$  is linear under single-collision conditions. Here,  $0.6 \mu\text{s}$  is the time of a single collision, and multiple collisions after  $0.6 \mu\text{s}$  do not obey the linear relationship. The representative number of data points is 40, and the step length varies (10 ns) based on the time scale of the profile. The slope of the fitting line yields the radiation rate.

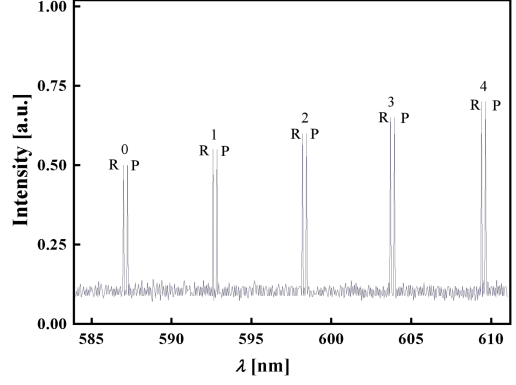


Fig. 3. Part of the dispersed fluorescence spectrum of the  $A(21, 10) \leftarrow X(33, 11)$  band of  $\text{Na}_2$ , indicating that the  $X(33, 11)$  ground state of  $\text{Na}_2$  was prepared.

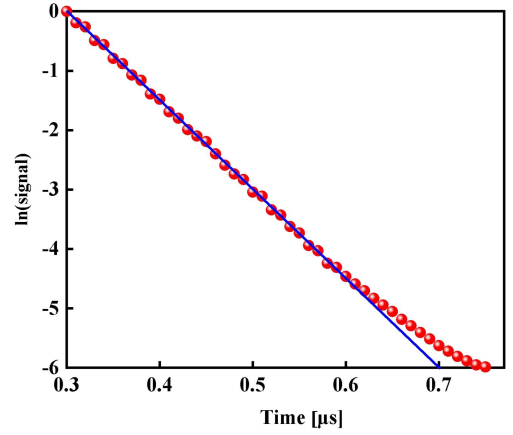


Fig. 4. Time-resolved fluorescence for the  $A(40, 10) \rightarrow X(45, 11)$  transition of  $\text{Na}_2$ ; the corresponding radiation rate is  $1.5 \times 10^7 \text{ s}^{-1}$  ( $T_{\text{cell}} = 670 \text{ K}$ ).

TABLE I

Average densities of the  $\text{Na}_2(v'' = 45, J'' = 11)$  states (in  $\text{cm}^{-3}$ ) for different  $T_{\text{cell}}$  values. Note: The numbers in the parentheses denote the  $2\sigma$  errors.

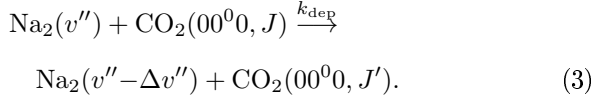
$T_{\text{cell}}$ [K]	$\text{Na}_2(45, 11)$
450	1.0(0.3)
523	2.1(0.6)
593	2.5(0.7)
670	3.3(0.8)
800	4.1(1.1)
900	4.9(1.3)

The nascent number density of the  $\text{Na}_2(v'', J'')$  states was determined from the absorption measurements at  $t = 1 \mu\text{s}$  during excitation with an OPO laser. Absorption coefficients and transient Doppler-broadening linewidths were used to convert the absorbed signals into  $\text{Na}_2(v'', J'')$  populations. The average densities of the  $\text{Na}_2(45, 11)$  state for different  $T_{\text{cell}}$  values are listed in Table I.

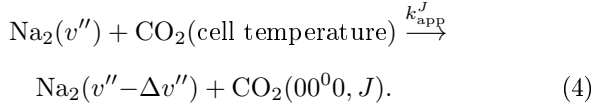
In Table I,  $\sigma$  is the uncertainty that was calculated using Excel based on the standard deviation of the experimental data obtained from multiple measurements.

### 3.2. Vibration–rotation energy transfer

The initial population of  $\text{CO}_2$  in the  $J$  state is depleted upon collision with the highly excited  $\text{Na}_2(v'')$  state according to the following transition [22]



Simultaneously, the  $\text{CO}_2$  molecules are scattered into the same  $J$ -state according to the transition below [22]



The population changes related to any collision that alters the initial state of rotation will cause depletion or appearance of  $J$ -specific for  $\text{CO}_2$ .

Nascent  $\text{CO}_2$  populations are determined from the intensity of the transient overtone LIF line measured at short intervals of time relative to the period between collisions [11]. Before recording the LIF intensities, the filter is removed. At a pressure of 15 mTorr, the collision time is around 4  $\mu\text{s}$  [6]. Thus, the transient intensity measurements were made at a time  $t = 1 \mu\text{s}$ , which is comparable to the average time of collisions between molecules. Such a short time corresponds to the scattered  $\text{CO}_2$  molecule populations, making secondary quenching collisions impossible.

### 3.3. Rotational distribution of $\text{CO}_2$

The proportion of the population at a level specified by  $J$  can be written in terms of the ratio of the transient intensities before and after excitation of the  $\text{Na}_2(v'')$  states, that is [23]

$$\frac{[\text{CO}_2(00^00, J)]_{t=1 \mu\text{s}}}{[\text{CO}_2(00^00, J)]_{t=0}} = \frac{I_{t=1 \mu\text{s}}^J}{I_{t=0}^J}, \quad (5)$$

where  $[\text{CO}_2(00^00, J)]_{t=0}$  is determined by the Boltzmann distribution according to [23]

$$[\text{CO}_2(00^00, J)]_{t=0} = [\text{CO}_2]_0 \frac{B(2J+1)}{k_B T} e^{-\frac{BJ(J+1)}{k_B T}}, \quad (6)$$

in which  $B = 0.394 \text{ cm}^{-1}$  is the rotational constant for  $\text{CO}_2$ . In turn,  $I_{t=0}^J$  is the transient intensity before excitation of the  $\text{Na}_2(v'')$  states, and  $I_{t=1 \mu\text{s}}^J$

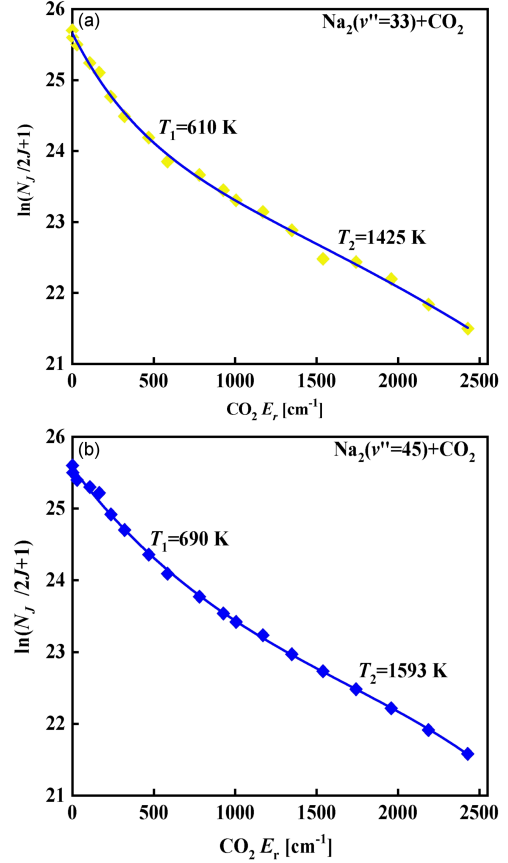


Fig. 5. Fitting of the nascent rotational distribution of  $\text{CO}_2$  using the two-component biexponential model described in (7).

denotes the  $(10^05, J) - (00^00, J)$  transition LIF intensity surveying at  $t = 1 \mu\text{s}$ . The time resolution of the LIF detection is 10 ns.

Figure 5 depicts the nascent rotation distribution of the scattered  $\text{CO}_2(00^00)$  molecules in collisions with  $\text{Na}_2(v'' = 33)$  and  $45$  at  $T_{\text{cell}} = 670 \text{ K}$ . A preferable profile of the nascent rotational distribution can be obtained using the sum of two separate distributions [10], that is [17]

$$[\text{CO}_2(J)] = (2J+1) \left( I_1 \exp\left(-\frac{BJ(J+1)}{k_B T_1}\right) + I_2 \exp\left(-\frac{BJ(J+1)}{k_B T_2}\right) \right). \quad (7)$$

Here,  $T_1$  and  $T_2$  are the rotational temperatures, and  $I_1$  and  $I_2$  are the relative intensities.

For the collisions with  $\text{Na}_2(v'' = 33)$ , the fitting yields a low-energy distribution for  $T_1 = 610 \pm 80 \text{ K}$  and a high-energy distribution for  $T_2 = 1425 \pm 150 \text{ K}$ . For the collisions with  $\text{Na}_2(v'' = 45)$ , the  $\text{CO}_2$  rotational temperatures are  $T_1 = 690 \pm 90 \text{ K}$  and  $T_2 = 1593 \pm 165 \text{ K}$ . The fact that  $T_1$  is very close to the inception point of 670 K in the distribution suggests that nearly elastic collisions are responsible

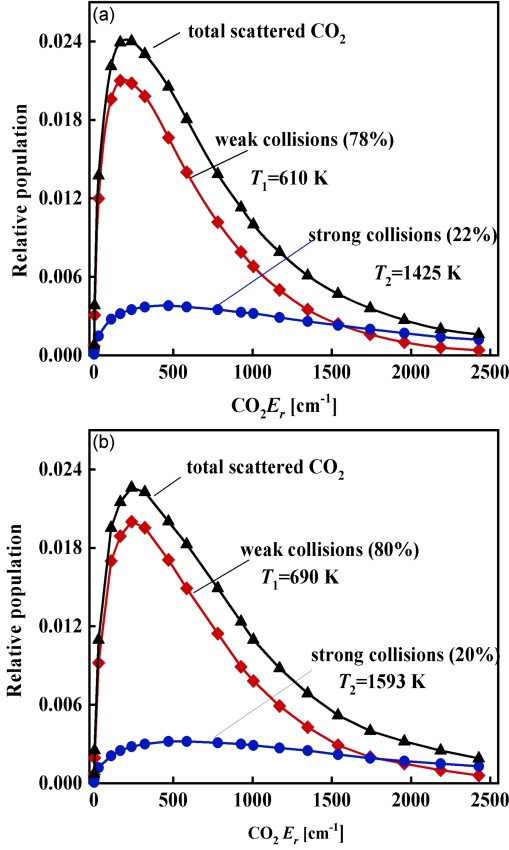


Fig. 6. Rotational distributions of the collisions with (a)  $\text{Na}_2(v'' = 33)$  and (b)  $\text{Na}_2(v'' = 45)$ . For both  $\text{Na}_2(v'')$  energies, the weak-collision pathway accounts for  $\sim 79\%$  of all collisions with the  $\text{CO}_2(00^0)$  products, while the strong-collision pathway accounts for  $\sim 21\%$  of these collisions.

for populating the low- $J$  final states. For comparison, the strong collisions that cause high-energy contrails are inelastic collisions causing a large increase in  $J$ .

Figure 6 depicts the rotational distribution for the collisions with the  $\text{CO}_2$  and  $\text{Na}_2(v'' = 33)$  and  $45)$  molecules. The combined strength of the weak-collision ingredient of  $\text{CO}_2$  accounted for 79% of the total number of collisions, while the high-energy ingredient accounted for 21%. Therefore, nearly four-fifths of the collisions involved only small changes in the rotation of  $\text{CO}_2$ , while the remaining one-fifth of the collisions resulted in significant changes in the rotational energy.

### 3.4. Translational temperature of $\text{CO}_2$

The nascent distribution of the recoil velocity for strong collisions is determined based on the LIF line for each  $\text{CO}_2$  rotational state. The shape of the LIF line for the  $\text{CO}_2(00^0, J = 62)$  state is shown in Fig. 7.

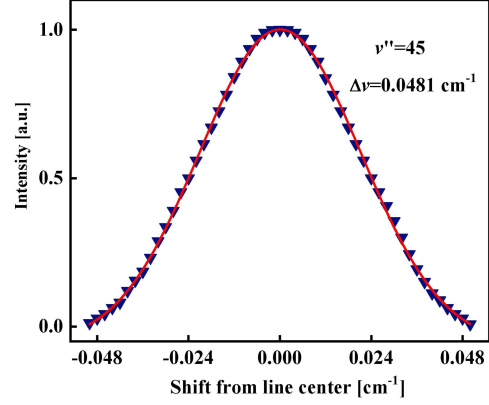


Fig. 7. Doppler-broadened transition line for  $\text{CO}_2(00^0, J = 62)$  collected at  $t = 1 \mu\text{s}$ , following the excitation of  $\text{Na}_2(v'' = 45)$  ( $T_{\text{cell}} = 670 \text{ K}$ ).

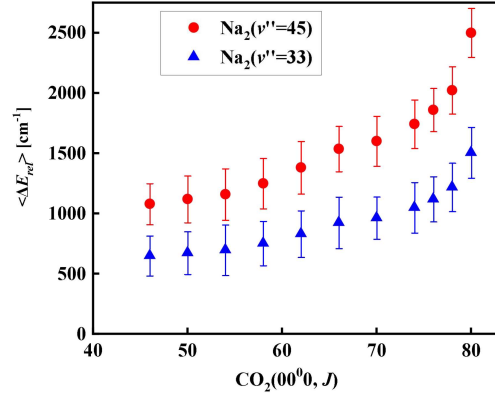


Fig. 8. Comparison of the nascent  $\langle \Delta E_{\text{rel}} \rangle$  values for the products of the collisions between the  $\text{CO}_2$  and  $\text{Na}_2(v'')$  molecules.

The full width at half maximum of the linewidth was found to be  $\Delta\nu = 0.0481 \text{ cm}^{-1}$ , which is equivalent to the velocity distribution of the laboratory frame at a translational temperature  $T_{\text{trans}}$  of  $1348 \pm 210 \text{ K}$ . The temperature of the laboratory frame was determined as  $T_{\text{trans}} = mc^2 / (8k_{\text{B}} \ln(2)) (\Delta\nu/v_0)^2$  [15], where the mass of  $\text{CO}_2$  is denoted as  $m$ , and the rovibrational transition frequency at the line center is denoted as  $\nu_0$ . The translational temperature corresponding to the center of mass was determined from the following relationship [15]

$$T_{\text{rel}} = T_{\text{trans}} + \frac{m_{\text{CO}_2}}{m_{\text{Na}_2}} (T_{\text{trans}} - T_0), \quad (8)$$

where  $T_0$  is the temperature of the cell. The variation in the mean translational energy of the center of mass due to the collisions of  $\text{Na}_2(v'')$  with  $\text{CO}_2$  is defined as  $\langle \Delta E_{\text{rel}} \rangle$  (in  $\text{cm}^{-1}$ ). The values of  $\langle \Delta E_{\text{rel}} \rangle$  can be established using the expression  $\langle \Delta E_{\text{rel}} \rangle = 1.5k_{\text{B}}(T_{\text{rel}} - T_0)$ . For  $\text{Na}_2(v'' = 45)$ , the temperature of the relative translational energy distribution for the  $J = 62$  state of  $\text{CO}_2$  is  $T_{\text{rel}} = 2000 \pm 316 \text{ K}$ , which corresponds to  $\langle \Delta E_{\text{rel}} \rangle = 1382 \pm 218 \text{ cm}^{-1}$ .

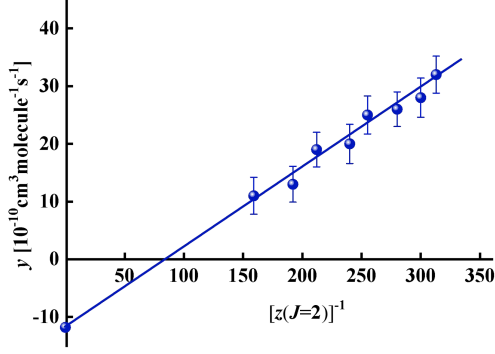


Fig. 9. Derivation of the rate constants  $k_{\text{app}}^{J=2}$  and  $k_{\text{dep}}$  for the collisions between  $\text{Na}_2(v'' = 45)$  and  $\text{CO}_2$ . The slope of the fitted line yields  $k_{\text{app}}^{J=2} = (1.4 \pm 0.3) \times 10^{-11} \text{ cm}^3/(\text{molecule s})$ . The intercept yields  $k_{\text{dep}} = (11.8 \pm 3.4) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$ .

TABLE II

Energy transfer rate constants  $k_{\text{app}}^J$  for the collisions between  $\text{Na}_2(v'')$  and  $\text{CO}_2$ . Note: This table represents a portion of the  $k_{\text{app}}^J$  values.

$J$	$k_{\text{app}}^J \times 10^{-12} [\text{cm}^3/(\text{molecule s})]$	
	$\text{Na}_2(v'' = 33)$	$\text{Na}_2(v'' = 45)$
2	$28 \pm 6$	$14 \pm 3$
8	$39 \pm 8$	$29 \pm 6$
22	$62 \pm 13$	$56 \pm 12$
28	$21 \pm 5$	$26 \pm 6$
34	$16 \pm 4$	$24 \pm 5$
40	$12 \pm 3$	$8.1 \pm 1.7$
46	$8.3 \pm 1.7$	$7.2 \pm 1.5$
58	$7.6 \pm 1.6$	$5.6 \pm 1.2$
64	$5.3 \pm 1.1$	$4.2 \pm 0.9$
70	$1.5 \pm 0.3$	$0.9 \pm 0.2$
78	$1.1 \pm 0.2$	$0.7 \pm 0.2$

The nascent energy dependence  $\langle \Delta E_{\text{rel}} \rangle$  values of the  $J = 46$ – $80$  states after a single collision between the  $\text{CO}_2$  and  $\text{Na}_2(v'')$  molecules with the vibrational states 33 and 45 are shown in Fig. 8. When the  $\text{Na}_2(v'')$  energy is high enough, the recoil energy of all  $J$  states also increases. The amount of energy converted to the translational energy rises with the donor energy. It was found that for every 25% increase in donor vibrational energy, the translational energy of a  $J$ -specific collision product increased by at least 60%.

### 3.5. Appearance and depletion rate constants

As shown in Fig. 5, the energy transfer rates of the  $J$ -state distribution determining the nascent appearance of some product states can be established according to (4) by combining the rate measurements and relative population experiments. In turn,

TABLE III

Rate constants corresponding to the depletion of the  $\text{CO}_2(00^0_0, J)$  states due to the collision with  $\text{Na}_2(v'')$ .

$J$	$k_{\text{dep}} \times 10^{-10} [\text{cm}^3/(\text{molecule s})]$	
	$\text{Na}_2(v'' = 33)$	$\text{Na}_2(v'' = 45)$
2	$12.1 \pm 3.5$	$11.8 \pm 3.4$
8	$10.5 \pm 3.1$	$9.7 \pm 2.8$
22	$9.6 \pm 2.8$	$8.8 \pm 2.6$
28	$8.5 \pm 2.5$	$5.3 \pm 1.5$
34	$3.2 \pm 1.0$	$2.7 \pm 0.8$
38	$1.3 \pm 0.4$	$1.1 \pm 0.3$
$\langle k_{\text{dep}} \rangle$	$7.5 \pm 2.2$	$6.6 \pm 1.9$

the  $J$ -specific rate constant  $k_{\text{app}}^J$  for the appearance of the  $\text{CO}_2(00^0_0, J)$  state is defined as [18]

$$\Delta[\text{CO}_2(00^0_0, J)]_{\text{app}} = k_{\text{app}}^J [\text{CO}_2]_0 [\text{Na}_2(v'')]_0 \Delta t, \quad (9)$$

where  $\Delta[\text{CO}_2(00^0_0, J)]_{\text{app}}$  is the appearance population with an initial  $\text{Na}_2(v'')$  concentration of  $[\text{Na}_2(v'')]_0$  states and an initial  $\text{CO}_2$  population of  $[\text{CO}_2]_0$  states;  $\Delta t = 1 \mu\text{s}$ .

The depletion rate of  $\text{CO}_2$  in a given state is described as [18]

$$\Delta[\text{CO}_2(00^0_0, J)]_{\text{dep}} = -k_{\text{dep}} z(J) [\text{CO}_2]_0 [\text{Na}_2(v'')]_0 \Delta t, \quad (10)$$

where  $k_{\text{dep}}$  is the depletion rate constant, and  $z(J)$  is the fraction of  $\text{CO}_2$  in a particular  $J$ -state. Using the first-order approximation, it is assumed that the depletion rate constant is independent of  $J$ .

By combining (9) and (10), it can be found that [18]

$$\frac{\Delta[\text{CO}_2(J)]_{\text{dep}} + \Delta[\text{CO}_2(J)]_{\text{app}}}{[\text{CO}_2(J)]_0 [\text{Na}_2(v'')]_0 \Delta t} = -k_{\text{dep}} + k_{\text{app}}^J z(J)^{-1}, \quad (11)$$

where  $z(J)^{-1} = [\text{CO}_2]_0 / [\text{CO}_2(J)]_0 = [B(2J+1)/(k_{\text{B}}T) \times \exp(-BJ(J+1)/(k_{\text{B}}T))]^{-1}$ ,  $T$  is the temperature in the cell, and  $\Delta t = 10^{-6}$  s. By substituting the observed LIF intensity for the population in (11), it is evident that [18]

$$y = \frac{10^6}{[\text{Na}_2(v'')]_0} \frac{I_0^J - I_{t=1\mu\text{s}}^J}{I_0^J} = -k_{\text{dep}} + k_{\text{app}}^J z(J)^{-1}. \quad (12)$$

Figure 9 depicts the functional relationship between the left-hand side of (12) and  $z(J)^{-1}$  as a straight line with a slope of  $k_{\text{app}}^J$  and an intercept of  $-k_{\text{dep}}$ . Tables II and III contain the measured  $k_{\text{app}}^J$  and  $k_{\text{dep}}$  values, respectively. The uncertainties in Tables II and III are treated the same way as the uncertainties in Table I.

The sum of the rate constants  $k_{\text{app}}^J$  ( $k_{\text{app}} = \Sigma k_{\text{app}}^J$ ) was used to determine the apparent rate constants of all  $\text{CO}_2$  product states. For the collisions with  $\text{Na}_2(v'' = 33)$ , it was found that  $k_{\text{app}} = (8.0 \pm 2.1) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$ . This result

is comparable to that obtained for Na<sub>2</sub>(*v*" = 45), for which the appearance rate constant is  $k_{\text{app}} = (6.9 \pm 1.8) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$ . For the collisions with Na<sub>2</sub>(*v*" = 33), the mean depletion rate of a low-*J* state is  $(7.5 \pm 2.2) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$ , which also approaches the depletion rate constant obtained for Na<sub>2</sub>(*v*" = 45), namely  $\langle k_{\text{dep}} \rangle = (6.6 \pm 1.9) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$ . The uniformity of the overall depletion and appearance rates for the two separate Na<sub>2</sub> energies indicates the significance of the V-RT energy transfer and confirms the fact that the collision rate constant of the system does not change with the donor energy.

#### 4. Conclusions

The excitation of Na<sub>2</sub> molecules to the vibrational states *v*" = 33 and *v*" = 45 was realized using SEP. The full-state resolved CO<sub>2</sub>(00<sup>0</sup>, *J*) molecules were produced when the excited Na<sub>2</sub> (*v*" = 33 and 45) collided with CO<sub>2</sub>(00<sup>0</sup>), exhibiting a biexponential rotational distribution. The biexponential distribution of the scattered CO<sub>2</sub> molecules indicated that 79% of the collisions were weakly inelastic, which had a minimal impact on the rotational motion of CO<sub>2</sub> upon scattering. The remaining collisions (21%) were strongly inelastic, and their higher energies significantly altered the rotational energy of CO<sub>2</sub>. It was found that for every 25% increase in donor vibrational energy, the translational energy of the *J*-specific collision product increased by 60% or more. The calculated average depletion and appearance rate constant for the collisions of Na<sub>2</sub>(*v*" = 33 and 45) with CO<sub>2</sub>(00<sup>0</sup>) were calculated to be  $(7.5 \pm 2.2) \times 10^{-10}$  and  $(6.6 \pm 1.9) \times 10^{-10} \text{ cm}^3/(\text{molecule s})$ , respectively.

#### Acknowledgments

This work was supported by the National Natural Science Foundation of China (grant No. 12164047) and the Natural Science Foundation of Xinjiang Uygur Autonomous Region (grant number 2023D01C06).

The authors also acknowledge Mogo Internet Technology Co., Ltd. (MogoEdit; <https://www.mogoeedit.com>) for providing manuscript editing service.

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