Vibrational Spectroscopic and Computational Studies on Bis(2-aminopyridinium)fumarate — Fumaric Acid (1:1) Complex

N. KANAGATHARA a,* , K. PAWLUS^b AND M.K. MARCHEWKA^b

^aDepartment of Physics, Saveetha School of Engineering, Saveetha Institute of Medical and Technical Sciences, Thandalum, Chennai 602 105, India

^bInstitute of Low Temperature and Structure Research, Polish Academy of Sciences, 50-950 Wrocław 2, Poland

(Received October 15, 2017; in final form November 15, 2017)

The new vibrational and computational studies on bis(2-aminopiridinium) fumarate — fumaric acid (1:1) complex have been made. The molecular geometry, vibrational frequencies and intensities of vibrational bands have been interpreted with the aid of structure optimization based on density functional theory (B3LYP) method with 6-311++G(d,p) basis set. The highly occupied—lowly unoccupied molecular orbital energies and chemical reactivity of the molecule have been calculated with time-dependent density functional theory approach. Stability energies of the molecule have been studied using natural bond orbital analysis. The predicted nonlinear optical properties of the title compound are much greater that those of urea. In addition, the molecular electrostatic potential surfaces and thermodynamic properties were calculated.

DOI: 10.12693/APhysPolA.133.45

PACS/topics: 2-aminopyridine, fumaric acid, DFT, FT-IR, FT-Raman

1. Introduction

The crystal structure of 2-aminopyrimidine-fumaric acid co-crystal was published by Goswami et al. [1] with the unit cell parameters a = 3.80, b = 19.18,c = 13.06 Å and $\beta = 96.89^{\circ}$. Later the crystal structure of the bis(2-aminopyridinium) fumarate — fumaric acid (1:1) (2APF-F) was published and deposited in the CSD database in 2002 by Ballabh et al. [2] and found that the compound crystallized in monoclinic system with $P2_1/c$ space group, the unit cell parameters are as follows: a = 10.47, b = 4.95 Å, c = 19.21 Å and $\beta = 102.14^{\circ}$. The carboxylate group of the 2APF-F interacts with the aminopyridinium cation through the pair of N-H...O hydrogen bonds and form an eightmembered R_2^2 (8) ring motif. This motif is one of the 24 most frequently observed bimolecular cyclic hydrogenbonded motifs in organic crystal structures. In 2013 Dong et al. [3] found the new polymorph of 2APF-F, which crystallized in triclinic system in centrosymmetric space group. In both polymorphs asymmetric units consist of one 2-aminopirydinium cation, half a fumaric acid molecule and half a fumarate dianion.

The fumaric acid is an organic dicarboxylic acid which is widely found in nature and it is also a key intermediate in the biosynthesis of organic acids. The fumaric and maleic acid are the simplest dicarboxylic acids exhibiting a carbon–carbon double bond. Both acids have important applications in polymer industry [4, 5] and also in medicine [6–9] as anti-fungicides and antitumor agents. Macoas et al. studied the spectroscopic and computa-

tional studies of (E)- and (Z)-buthenedioic acids [10]. The heteroaromatic pharmaceuticals containing nitrogen (like pyridine) are very popular in the resent days. The aminopyridine molecules are mainly used as the starting materials in the production of various drugs. The aminopyridine and derivatives are used in the synthesis of pharmaceuticals especially for antihistamines, antiinflammatories drugs. The Fourier transform infrared (FT-IR) and the Raman spectra of pure 2-aminopyridine were studied by Mohan and Ilangovan [11]. The fumaric acid and 2-aminopyridine could be proton donor and/or acceptor and are widely used in crystal engineering to obtain the structures with rich hydrogen bonds network. The excellent hydrogen bond network in this combination makes it suitable for NLO applications [12]. The weak intermolecular interactions, like hydrogen bonds cause significant changes in the vibrational spectra [13]. In addition in the crystals are symmetrically spread molecules which can cause some kinds of splitting [14]. These effects make the spectra of the solids differ from spectra of liquids or gases. It is known that vibrational (IR and Raman) spectroscopy would be a suitable method to study hydrogen-bonded complexes in crystalline form.

In this communication, the detailed assignment of vibrational studies of 2APF-F is discussed by both theoretical and experimental results. Density functional theory (DFT) calculations are used in order to perform structural analysis of the title molecule. Additionally, the non-linear optical properties, frontier orbitals, molecular electrostatic potential, interaction energies (NBO) and statistical thermodynamic properties have been investigated using B3LYP method.

2. Experimental

The starting compounds, 2-aminopyridine (Merck, $\geq 98\%$) and fumaric acid (Merck, $\geq 99\%$), were used with-

^{*}corresponding author; e-mail: kanagathara232750gmail.com

out any further purification. Compounds were dissolved in doubly distilled water in equimolar amounts. Then the solution was purified with the aid of charcoal and allowed to evaporate at room temperature. Crystals of bis(2-aminopyridine) fumarate — fumaric acid (1:1) appeared after a month.

3. Characterization

The X-ray diffraction data were collected on a four circle KUMA KM-4 diffractometer equipped with a twodimensional area CCD detector. The graphite monochromatized Mo K_{α} ($\lambda = 0.71073$ Å) and ω -scan technique with $\Delta \omega = 0.75^{\circ}$ for one image were used for data collection. Integration of the intensities, correction for Lorentz and polarization effects was performed using KUMA KM-4 CCD software [15]. The crystal structure was solved by a direct method and subsequent difference Fourier syntheses of SHELXL-PLUS program system [16] and the structure was refine by use of SHELXL 97 [17]. Anisotropic displacement parameters were included for all non-hydrogen atoms. The spectroscopic measurements were carried out at room temperature, in the region $4000-80 \text{ cm}^{-1}$. The powder infrared spectra were measured using Bruker IFS-88 spectrometer with resolution 2 cm^{-1} , signal/noise ratio were established by 32 scans. The samples in Nujol and Fluorolube suspensions were used to eliminate the bands originating from the oils. Powder Fourier transform Raman spectra were taken with an FRA-106 attachment to the Bruker IFS-88 spectrometer equipped with Ge detector cooled to liquid nitrogen temperature. Nd⁺³:YAG air-cooled diode pumped laser of power ca. 500 mW was used as an excitation source. The incident laser excitation was 1064 nm. The scattered light was collected at the angle 180° in the region $3600-80 \text{ cm}^{-1}$, resolution 2 cm^{-1} , 32 scans.

4. Computation details

The DFT has long been recognized as a better alternative tool in the study of organic, inorganic chemical system. In the present study, DFT calculations were performed by DFT-B3LYP method with 6-311++G(d,p)basis set using Gaussian 09 program [18], under the calculation grant at WCSS (WCSS#106602). The single crystal X-ray diffraction experimental results are given as input to the Gaussian program to obtain the molecular geometry. Vibrational frequencies were scaled by 0.9613 [19]. The assignment of the calculated normal modes has been made on the basis of the corresponding PEDs. The PEDs are computed with quantum mechanically calculated vibrational frequencies using VEDA program [20]. The energy gap value between the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) energies was also calculated. The chemical reactivity was also calculated by IEF-PCM method in one solvent-water ($\varepsilon = 78.39$). Electrostatic potential energy surface map is employed to convey the varying intensities of the electrostatic potential energy values. The polarizability α , dipole moment μ and first order hyperpolarizability β are calculated using B3LYP/6–311++G (d,p) basis set on the basis of the finite-field approach. The NBO analysis was performed at the B3LYP/6-311++G(d,p) level of theory by means of the NBO 3.1 [21] program within the Gaussian 09 package.

5. Results and discussion

5.1. Structural analysis

The obtained crystal crystallizes in the monoclinic system with $P2_1/c$ space group. The lattice constants are: a = 10.387(18) Å, b = 4.926(10), c = 19.148(19), $\alpha = \gamma = 90^{\circ}$, $\beta = 101.61(10)^{\circ}$. Other crystallographic parameters are collected in Table I. Atoms numbering scheme is

Crystallographic data of 2APF-F crystal TABLE I

	[10]	[11]	Exp.
Formula	$C_9H_{10}N_2O_4$	$\mathrm{C}_{18}\mathrm{H}_{20}\mathrm{N}_{4}\mathrm{O}_{8}$	$C_9H_{10}N_2O_4$
М	210.19	420.38	210.19
crystal system	monoclinic	triclinic	monoclinic
space group	$P2_{1}/c$	<i>P</i> -1	$P2_{1}/c$
a [Å]	10.467(3)	3.816(7)	10.387(18)
b [Å]	4.947(2)	9.606(3)	4.926(10)
c [Å]	19.211(3)	13.360(4)	19.148(19)
α [°]	90	94.287(15)	90
β [°]	102.14	91.743(14)	101.61(10)
γ [°]	90	91.716(14)	90
V [Å ³]	972.5(5)	488.02(3)	957.5(2)
Ζ	4	1	4
T [K]	293	298	210(2)



Fig. 1. Molecular structure of 2APF-F: (a) experimental (b) theoretical.

Selected molecular structure parameters. TABLE II					
	Exp. [1]	B3LYP/6-311++0	G(d.p)		
	Bond	l length [Å]			
O3_C8	1.271(2)	1.272			
C8–O4	1.249(2)	1.250			
C8–C9	1.497(2)	1.506			
C9–H10	0.94(2)	1.085			
C9–C9B	1.315(2)	1.335			
H2–O2	1.04(3)	1.083			
O2–C1	1.314(2)	1.342			
C1–O1	1.210(2)	1.210			
C1-C2	1.492(2)	1.483			
C2-H1	0.95(2)	0.969			
C2-C2B	1.303(2)	1.333			
H9-N2	0.92(2)	1.005			
H6-N2	0.89(2)	1.044			
N2-C3	1.328(2)	1.338			
N1-H5	0.93(2)	1.114			
C7-N1	1.361(2)	1.352			
N1-C3	1.353(2)	1.357			
C7-C6	1.354(3)	1.370			
C6-C5	1.399(3)	1.409			
C5-C4	1.358(3)	1.374			
C3-C4	1.415(2)	1.419			
C7-H4	1.02(2)	1.082			
C6-H7	0.94(2)	1.080			
C5-H3	0.95(2)	1.083			
C4-H8	0.98(2)	1.082			
Max. differen	ce^a [Å] 0.1	184 N1–H5			
	Bond	angles [°C]			
O3–C8–O4	123.5(1)	126.35			
O4–C8–C9	118.9(1)	118.76			
C8–C9–C9B	123.6(1)	122.29			
H10-C9-C8	115(1)	116.40			
H2–O2–C1	114(2)	107.90			
O2-C1-O1	124.7(1)	123.04			
C1-C2-C2A	123(2)	120.94			
H1-C2-C1	115(1)	118.00			
H6–N2–H9	123(2)	119.66			
H9–N2–C3	118(1)	119.08			
N2-C3-C4	123.4(1)	123.90			
N1-C3-C4	117.4(1)	118.01			
H8-C4-C5	125(1)	121.39			
C5-C4-C3	120.1(2)	119.75			
Max	c. difference	e^{a} [°] 6.1 H2–O2–C1			

 a Maximum differences between the bond lengths and angles computed using theoretical methods and those obtained from X-ray diffraction.

presented in Fig. 1a. The asymmetric unit cell of [2APF-F] contains one 2-aminopyridine cation, half of the fumarate dianion and half acid molecule — both are located in the centers of symmetry. The structure is stabilized by hydrogen bonding. Hydrogen bond in 2APF-F crystal structure is shown in Fig. 2. Crystal structure revealed that the dianion is involved in complementary dimeric hydrogen bonding interactions with two 2-aminopyridinium



Fig. 2. Hydrogen bonds in 2APF-F crystal structure.

cations and such assemblies are held together by N– H...O hydrogen bonding in a staircase fashion. Dianions and the acid molecules form hydrogen bonds O–H...O thereby form chains extending along a ($C_0^2(6)$ considering the dianion or $C_2^0(8)$ considering the free acid, graph set representation). The 2-aminopyridinium cations sit in between the chains through N–H...O and C–H...O hydrogen bonds ($R_2^3(8)$ and $R_2^2(8)$ graph set representation). In this way a 2D hydrogen bonded sheet along the *ac*-plane is made.

TABLE III

$\mathrm{D}\text{-}\mathrm{H}\cdots\mathrm{A}$	$d(\mathbf{H} \cdots \mathbf{A})$	$d(\mathbf{D}\cdots\mathbf{A})$	\angle (D-H···A)				
$O2-H2\cdots O3^a$	1.58	2.61	175.0				
$\rm N1\text{-}H5{\cdots}O3$	1.84	2.77	174.8				
$N2-H9\cdots O4$	1.99	2.86	164.6				
$N2-H6\cdots O2^{b}$	2.03	2.94	166.0				
$C7-H4\cdots O1^{c}$	2.18	3.18	167.8				
a:-x+1, y-0.5, -z+0.5; b:-x, y-0.5, -z+0.5;							
c:-x+1, y+0.	c:-x+1, y+0.5, -z+0.5						

Hydrogen bonds of 2APF-F. d [Å], \angle [°].

The optimized geometrical parameters of bis(2aminopyridine) fumarate — fumaric acid (1:1) are obtained using B3LYP/6-311++G(d,p) method and the results are listed in Table II. The atomic numbering scheme of the theoretical molecular structure of the studied compound is shown in Fig. 1b. As seen from Table II, most of the bond lengths are insignificantly longer than the experimental values and the bond angles are slightly smaller from experimental ones. It should be noted that experimental results belong to solid phase and theoretical computations belong to the gas phase. The comparison reveals that there are no big differences between these two structures. Table III lists the hydrogen bonds of 2APF-F. The N-H...O, O-H...O and C-H...O hydrogen bonds are formed between cations and dianions, dianions and fumaric acid molecules. In the optimized geometry only intramolecular hydrogen bonds are created between 2-aminopyridine cation and fumarate dianion. The biggest difference in bond lengths ≈ 0.184 Å is found

in H5–N1 bond between the experimental and the predicted value. The biggest difference for the bond angles is found as 6.1° at H2–O2–C1. The biggest differences of bond lengths and bond angles mainly occur in the groups involved in the hydrogen bonds, which can be also easily understood by taking into account the intermolecular interactions present in the crystal.

5.2. Vibrational analysis

The optimized structural parameters were used to compute the vibrational frequencies of 2APF-F by using B3LYP/6-311++G(d,p) method. The experimental vibrational spectra for normal and deuterated crystals are shown in Figs. 3 and 4, respectively. The total num-



Fig. 3. Experimental (a) and deuterated analogue (b) FT-IR spectrum of 2APF-F.



Fig. 4. Experimental (a) and deuterated analogue (b) FT-Raman spectrum of 2APF-F.

ber of vibrations of 2APF-F consists of 96 external vibration (vibration of crystal lattice) and 504 internal vibrations. Table IV summarizes the internal and external vibrations. According to the selection rules, 252

Fundamental external and internal vibrational analysis of 2APF-F.

C	Ext.		Int.			Select. rules		
O_{2h}	T_a	Т	R	D	С	Α	IR	Raman
A_g		12	12	24	72	30		xx.yy.zz.xy
B_g		12	12	24	72	30		xz.yz
A_u	1	11	12	24	72	30	z	
B_u	2	10	12	24	72	30	x.y	

 T_a — acoustic; T — translational; \overline{R} — librations; D fumarate dianion C_i ; C — 2-aminopyridine cation C_1 ; A — fumaric acid C_i .



Fig. 5. Theoretical FT-IR and FT-Raman spectrum of 2APF-F.

internal vibrations should be observed in the IR spectrum and 252 on the Raman spectra. As shown on the IR and Raman spectra the number of vibration it is much smaller. This may be the result of applying vibrations of similar energies. The bands observed in the region 4000–200 $\rm cm^{-1}$ arise from the vibrations of protons in the hydrogen bonds, the internal vibrations of 2aminopyridine cations, fumarate anions and fumaric acid. The bands below 200 cm^{-1} arise from the lattice vibrations of the crystal. Theoretical FT-IR and FT Raman spectra (Fig. 5) are interpreted by means of PEDs using VEDA program [20]. The observed FTIR, FT-Raman and calculated frequencies determined by B3LYP method with 6-311++G(d.p) basis set along with relative intensities, probable assignments and potential energy distribution (PED) are listed in Table V. The Raman intensities derived from the computed Raman activities using the equation

$$I_i^R = C(v_0 - v_i)^4 v_i^{-1} B_i^{-1} S_i,$$

where $v_0 = 9398.5 \text{ cm}^{-1}$ (1064 nm), $B_i = 1 - \exp(-hv_i c/kT)$, v_i is the frequency of normal mode $[\text{cm}^{-1}]$, S_i is the Raman activity of the normal mode, h— the Planck constant [eV/s], k— the Boltzmann constant [eV/K], c— speed of light [cm/s], T— temperature in K— 298.15 K [22].

The observed FTIR, FT-R(aman) $[cm^{-1}]$ and calculated frequencies determined by B3LYP method with 6-311++G(d.p) basis set along with relative intensities. probable assignments and potential energy distribution (PED). A — bis(2-aminopyridine) fumarate — fumaric acid (1:1), B — deutered bis(2-aminopyridine) fumarate — fumaric acid (1:1), C — scaled calculated wavenumbers [cm], D — IR intensity, E — Raman activity.

A FTIR	FT-B	B FTIR	FT-B	С	D	Е	PED [%]	Assignment
				3609	41.36	192.56	$\Omega_{2}-H_{2}(91)$	OH stretch
				3608	169.51	63.32	O2A-H2A(91)	OH stretch
				3532	169.51	63.32	$N_{2}-H_{6}(59)$ $N_{2}-H_{9}(41)$	NH ₂ asym
				0002	100.01	00.02		stretch
	3121 m	3127 w		3102	79.63	97.26	C4-H8, C6-H7, C5-H3, C7-H4(93)	CH (arom.) stretch
		3100 m	$3103~{\rm s}$	3077	0.55	245.51	C4-H8, C6-H7, C5-H3, C7-H4(91)	CH (arom.) stretch
$3093~\mathrm{m}$		3087 w	$3089 \mathrm{~s}$	3075	2.65	66.73	C4-H8, C6-H7, C5-H3, C7-H4(99)	CH (arom.) stretch
		3070 w		3073	1.31	159.39	C2-H1, C2A-H1A(99)	CH stretch
				3069	1.19	0.28	C2-H1, C2A-H1A(99)	CH stretch
				3060	0.04	133.37	C4-H8, C6-H7, C5-H3, C7-H4(92)	CH (arom.) stretch
				3058	1.62	67.39	C9-H10, C9A-H10A(99)	CH stretch
$3055~\mathrm{m}$	$3056 \mathrm{~s}$		$3056~{\rm s}$	3054	1.22	15.59	C9-H10, C9A-H10A(99)	CH stretch
	$3036 \mathrm{m}$		$3035 \mathrm{~s}$					CH stretch
				2860	2862.33	174.99	N2-H9, N2-H6(97)	NH ₂ sym stretch
2600 b m		2636 vw						$OH \cdots O$ stretch
		1950 b m						$OD \cdots O$ stretch
$1900~\mathrm{b}~\mathrm{m}$				1919	3786.38	67.86	N1-H5(65), O3-H5(10)	$NH \cdots O$ stretch
				1728	128.82	76.74	O1-C1, O1A-C1A(84)	C=O stretch
1700 vw	$1706 \mathrm{m}$		$1702~\mathrm{m}$	1708	740.06	35.07	O1-C1, O1A-C1A(83)	C=O stretch
		$1698 \mathrm{~s}$		1695	268.83	5.11	O3-H5(33), O1-H3(20), N1-C3, N2- C3, N1-C7(12)	$NH \cdots O$ stretch
$1675~\mathrm{vs}$	$1660~\mathrm{vs}$	$1669 \mathrm{~s}$	$1659~\mathrm{vs}$					C-N stretch
		1649 vs		1645	1.09	227.7	H1-C2-C1, H1A-C2A-C4(15), C7-C4(67), C1-C2, C1A-C2A(11)	C=C (arom.) stretch
				1643	170.83	6.24	H9-N2-H6(53), H6-N2-C3(23)	NH ₂ bending in plane
$1638~\mathrm{vs}$	$1636~{\rm s}$		$1635 \mathrm{~m}$	1629	5.26	155.17	H10-C9-C9A, H10A-C9A-C9(15), C9-C9A(67), C8-C9, C8A-C9A(10)	C=C stretch
		1593 vs	$1595~\mathrm{m}$	1605	100.52	8.43	C4-C5, C5-C6, C7-C6(45)	C=C (arom.) stretch
$1553~\mathrm{m}$	$1557~\mathrm{m}$	1552 vs						C=C stretch
$1538~{\rm s}$		1535 vs	1533 w					$ \begin{array}{ccc} \mathrm{NH}_2 & \mathrm{bending} & \mathrm{in} \\ \mathrm{plane} & \end{array} $
			1531 w	1523	1.79	19.51	C4-C5, C5-C6, C7-C6(28), C4-C5-C6, C7-C6-C5(13), N1-C7-C6, N2-C3-C8, C3-N1-C7(14)	$egin{array}{c = C \ (arom.) \ stretch \ + \ NC \ bend \end{array}$
$1492~{\rm s}$	$1492~\mathrm{m}$		$1496~\mathrm{vw}$	1502	729.4	30.7	C3-C8, O3A-C8A, O4-C8, O4A- C8A(21), C7-N1, C3-N1(10)	COO ⁻ asym stretch
$1382~{\rm s}$	$1383~{\rm s}$		1384 m	1487	371.42	27.16	O3-C8, O4-C8, O3A-C8A, O4A-C8A(36), C9-C8, C8A-C9A(11)	COO ⁻ sym stretch
		1459 m	1460 w	1454	3.53	8.1	H3-C5-C6, H4-CC7-C6, H7-C6-C7, H8-C4-C5(19)	HC (arom.) bend
1436 m	1433 vw		1400 m	1411	20.16	7.15	H3-C5-C6, H4-CC7-C6, H7-C6-C7, H8-C4-C5(28), N1-C3, N1-C7, N2- C3(22)	HC bending
$1368~\mathrm{vs}$		$1376 \mathrm{~s}$						C-O stretch

								TABLE V (cont.)
A	FT-B	FTIR	B FT-B	С	D	Е	PED [%]	Assignment
1340 m		1340 vs		1342	44.38	26.5	C4-C5, C6-C5, C7-C6(19), H3-C5- C6, H4-CC7-C6, H7-C6-C7, H8-C4- C53(18), N1-C3, N1-C7, N2-C3(16)	CC bending
	$1337 \mathrm{~m}$			1337	1010.66	13.86	O3-C8, O4-C8, O3A-C8A, O4A-C8A(27)	C-O stretch
			1319 s	1323	327.02	0.07	C1-O2, O2A-C1A(20), C1-C2, C1A- C2A(18), H1-C2-C1, H1A-C2A-C2(16), H2-O2-C1(16), H2A-O2A-C1A(10)	C-C in plane bending
				1311	6.12	3.3	H1-C2-C1, H1A-C2A-C2(19), H2A- O2A-C1A(17), C2A-C2(12), O2-C1, O2A-C1A(17)	
1282 s				1300	61.18	15.8	H3-C5-C6, H4-C7-C6, H7-C6-C7, H8- C4-C5(22), C4-C5, C6-C5, C7-C6(14), H6-N2-C3(14), N1-C3, N1-C7, N2- C3(10)	C-H in plane bending (sciss.)
1261 s	1264 s		1269 m	1247	18.38	1.55	N1-C3, N1-C7, N2-C3(29), H10-C9- C9A, H10A-C9A-C8A(21), H3-C5-C6, H4-C7-C6, H7-C6-C7, H8-C4-C5(15)	
			1248 m	1241	142.6	43.63	H10-C9-C9A, H10A-C9A-C8A(48), N1- C3, N1-C7, N2-C3(13)	CH bending
	$1237 \mathrm{~m}$			1237	0.12	15.85	H2-C2-C1, H1A-C2A-C2(50), H2A- O2A-C1A(13), H2-O2-C1(12)	C-H in plane bending (sciss.)
				1202	153.48	0.06	H2-C2-C1, H1A-C2A-C2(51), H2-O2- C1(19), H2A-O2A-C1A(19)	C-H in plane bending (rocking)
1192 m		1194 s		1199	50.15	0.33	O4-C8-O7-H5(42), O3-H5-N1-C3(29), H5-N1-C7-C6(22), C8-O3-H5-N1(18)	NH···O bend
$1172 \mathrm{~s}$	1162 m	$1178 \mathrm{~s}$	1162 w	1186	44.71	8.23	H10-C9-C9A, H10A-C9A-C8A(79)	CH bend in plane
	1140 m		1149 w	1135	24.5	20.41	H3-C5-C6, H4-C7-C6, H7-C6-C7, H8- C4-C5(73), C4-C5, C6-C5, C7-C6(14)	CH (arom.) in plane bending
				1120	17.12	13.73	$\begin{array}{c} \text{O2-C1, O2A-C1A(49), H2-O2-C1(18),} \\ \text{H2A-O2A-C1A(12)} \end{array}$	OH in plane bending
			1108 vw	1106	1.02	8.71	H3-C5-C6, H4-C7-C6, H7-C6-C7, H8- C4-C5(28), C4-C5, C6-C5, C7-C6(17), H6-N2-C3(14)	CH (arom.) in plane bending
1075 vw	1080 w			1091	587.14	0.2	O2-C1, O2A-C1A(41), H1-C2-C1, H1A- C2A-C2(27), H2A-O2A-C1A(13)	O-H in plane bending
		1068s		1071	44.38	42.66	O3-C8, O4-C8, O4A-C8A, O3A- C8A(49), O3-C8, O4-C8, O4A-C8A, O3A-C8A(34)	COO ⁻ in plane bending
			1055 w	1045	10.38	9.33	H6-N2-C3(33), H3-C5-C6, H4-C7- C6, H7C6-C7, H8-C4-C5(13), H9- N2-H6(13), N1-C7-C6, N2-C3-C4, C3-N1-C7(10)	NH in plane bending
$1030~{\rm w}$	1031 m			1010	3.47	14.01	C4-C5, C6-C5, C7-C6(57)	CC (arom.) stretch
		995 w	996 w	983	25.24	0.03	H1-C2-C1-O1, H1A-C2A-C2-C1(61), H3-C5-C6-C7, H4-C7-C6-C5, H7-C6- C7-N1, H8-C4-C5-C6(20)	CH out of plane bending
987 m	989 w			981	16.87	0.09	H3-C5-C6-C7, H4-C7-C6-C5, H7-C6- C7-N1, H8-C4-C5-C6(59), H1-C2-C1- O1, H1A-C2A-C2-C1(33)	CH out of plane bending
	976 w	976 s	975 w	980	40.96	0.64	H10-C9-C9A-C8A, H10A-C9A-C8A- O3A(95)	CH bending in plane
963 m		$967 \mathrm{~s}$		939	286.68	15.17	N1-C7-C6, N2-C3-C4, C3-N1-C7(27), C4-C5-C6, C7-C6-C5(20)	C-N in plane bending
			946 vw	933	2.18	1.33	H3-C5-C6-C7, H4-C7-C6-C5, H7C6- C7-N1, H8-C4-C5-C6(77)	

FTIR	FT-R	FTIR	FT-R	С	D	Е	PED [%]	Assignment
924 m				929	0.12	7.04	C1-C2, C1A-C2A(41), H1-C2-C1, C1A- C2A-C2(17), H1A-C2A-C2(10)	CC bending
				927	33.95	32.21	C9-C8, C9A-C8A(36), O3-C8, O4- C8, O3A-C8A, O4A-C8A(16), C9A-C9- C8(12)	CC bending
				920	72.37	49.65	C9-C8, C9A-C8A(59), O3-C8, O4-C8, O3A-C8A, O4A-C8A(23)	CC stretch
	908 w		908 w	896	0.1	7.32	H1-C2-C1-O2, H1A-C2A-C2-C1(72), C2A-C2-C1-O1(13), O1A-C2A-O2A- C1A(10)	HC=CH out of plane bending
	891 w			888	0.34	6.91	H10-C9-C9A-C8A, H10A-C9A-C9- C8(63), C9-O4-O3-C8(19)	HC=CH out of plane bending
		886 m	891 w	882	6.18	0.19	C1-C2, C1A-C2A(61), O2-C1, O2A- C1A(28)	C-O bending
$874 \mathrm{~w}$			868 w	867	34.63	0.54	H9-N2-H6-O4(64), H6-N2-C3-N1(14)	NH bending out of plane
$853~\mathrm{vw}$	855 vs							C-O bending
		834 vw	835 vs	831	8.1	35.74	C4-C5-C6, C7-C6-C5(21), N1-C7, N1- C3, N2-C3(20), N1-C7-C6, N2-C3-C4, C3-N1-C7(11)	CN bending
$805 \mathrm{m}$	805 vw	806 w		821	13.12	0.36	H3-C5-C6-C7, H4-C7-C6-C5, H7C6- C7-N1, H8-C4-C5-C6(82)	C=C (arom.) bending
$779~{\rm s}$	780 vw	$785 \mathrm{m}$	783 vw	761	63.79	0.04	O1A-C2A-O2A-C1A(43), O2-C2-O1- C1(44), C1A-C2A-C2-C1(10)	COOH out of plane bending
733 m		759 m		752	95.85	0.12	H3-C5-C6-C7, H4-C7-C6-C5, H7C6- C7-N1, H8-C4-C5-C6(67), N2-N1-C4- C3(15)	C=C (arom.) bending
723 w				746	4.48	0.01	O4A-C9A-O3A-C8A(32), C9-O4-O3- C8(37)	COO ⁻ out of plane bending
	710 vw			709	4.3	0.18	N2-N1-C4-C3(25), N1-C7-C6-C5, C3- N1-C7-C6(23), H3-C5-C6-C7, H4-C7- C6-C5, H7C6-C7-N1, H8-C4-C5-C6(13)	NC bending
		703 m		708	44.05	40.04	O4-B8-O3, O4A-C8A-O3A(55), O4-B8- O3, O4A-C8A-O3A(11)	COO ⁻ in plane bending
$691 \mathrm{m}$		$685 \mathrm{~s}$						O–HO out of plane bending
				667	0.7	2.6	O2-C2-O1-C1(30), O1A-C2A-O2A- C1A(29), H2A-O2A-C1A-C2A(18), H2-O2-C1-C2(14)	COOH out of plane bending
639 m				649	0.14	12.74	O1A-C1A-O2A(30), O2-C1, O2A- C1A(22), O2-C1-O1(19)	COOH in plane bend
$627 \mathrm{~m}$	$625 \mathrm{m}$	$613 \mathrm{~s}$	618 m	608	159.34	17.18	C4-C5-C6, C7-C6-C5(24), N1-C7-C6, N2-C3-C4, C3-N1-C7(31)	C=C (arom.) bend
				597	2.24	1.16	O4A-C9A-O3A-C8A(47), C9-O4-O3- C8(25), H10-C9-C9A-C8A, H10A-C9A- C9-C8(11)	C-O out-of plane bending
				591	70.74	130.07	O4-C8-O3, O4A-C8A-O3A(64), O4-C8- O3, O4A-C8A-O3A(13)	COO^- wagging
				582	196.79	0.03	H2A-O2A-C1A-C2A(51), H2-O2-C1- C2(45)	C-O bending
	$558 \mathrm{~s}$	$559 \mathrm{~m}$		581	90.03	0.23	O1A-C1A-O2A(40), O2-C1-O1(23), C2-C1-O1(16)	OH out of plane bending
$550 \mathrm{m}$				543	79.38	9.16	C9-C8-O3(29), O3A-C8A-C9A(16), N1- C7-C6, N2-C3-C4, C3-N1-C7(11)	C-C in plane bending
		543 w	545 m	539	24.23	2.26	N1-C7, N1-C3, C3-N2(19), N1-C7-C6, N2-C3-C4, C3-N1-C7(17), C9-C8-O3(12)	ring bending in plane
				532	0.79	1.76	H2-O2-C1-C2(39), H2A-O2A-C1A- C2A(29), O2-C2-O2-C1(12), O1A- C2A-O2A-C1A(10)	O-H out-of-plane bending

TABLE V (cont.)

A	ł]	В	C	п	E	PED [%]	Assignment
FTIR	FT-R	FTIR	FT-R		D	Ľ		Assignment
$525 \mathrm{m}$				523	48.55	0.12	O2A-C1A-C2A(34), C2-C1-O1(21), O2-C1-O1(18), C2A-C2-C1(10)	C-C in plane bending
		510 w		511	28.51	0.03	N1-C7-C6-C5(27), C4-C5-C6-C7(22), N2-N1-C4-C3(16)	ring out-of-plane bending
433 m	434 m	434 w		419	29.37	3.61	N1-C7-C6(24), O3A-C8A-C9A(16)	$ m NH_2$ in plane bending
				407	36.97	6.31	O3A-C8A-C9A(20), C8-C9(13), N1-C7-C6(11), C9-C8-O3(10)	COO^- bending
392 vw	396 vw		391 w	393	1.04	0.64	C4-C5-C6-C7(53), N1-C7-C6-C5(38)	
				374	98.69	0.49	H6-N2-C3-N1(30), C4-C5-C6-C7(18)	C-N out-of-plane bending
				355	0.33	1.2	O2A-C1A-O1A(33), O2-C1-O1(19), C2-C1-O1(18), C1-C2(16)	
	290 vw		289 w	289	45	8.58	C9A-C9-C8(24), C8-O3-H5(14), O3A- C8A-C9A(11)	
241 m				261	0.12	3.26	C1-C2(18), C2A-C2-C1(23), C2-C1- O1(17), C1A-C2A-C2(22)	
$195 \mathrm{m}$				198	0.67	0.37	N1-C7-C6-C5(38), C4-C5-C6-C7(17), N2-N1-C4-C3(10)	lattice vibrations
$182~\mathrm{m}$				191	64.29	1.3	O3-H5(38), C9A-C9-C8(14)	lattice vibrations
				153	5.75	0.22	C8A-C9A-C9-C8(66), O4A-C9A-O3A- C8A(10)	lattice vibrations
				147	10.82	1.88	C8-O3-H5(24), C8A-C9A-C9(33), O3A- C8A-C9A(12)	lattice vibrations
				139	0.04	0.06	C1A-C2A-C2-C1(74)	lattice vibrations
137 w	132 vs		131 vs	135	0.02	1.06	O2A-C1A-C2A-C2(44), C2A-C2-C1- O1(27), C1A-C2A-C2-C1(12)	
$122~{\rm w}$				123	2.8	0.03	C2A-C2-C1(38), C2-C1-O1(10)	lattice vibrations
				115	1.15	0.52	C9A-C9-C8-O4(54), C4-C5-C6-C7(13)	lattice vibrations
	107 vs		104 vs	102	13.64	3.01	H5-N1-C7(34), O3-H5-N1(27), H5- O3(12), C8-O3-H5(11)	lattice vibrations
99 w	$87 \mathrm{s}$		$85 \mathrm{s}$	83	0.85	5.22	H5-N1-C7-C6(32), O3A-C8A-C9A-C9(12)	lattice vibrations
b — bro	bad, vs –	– very s	trong, s	— s	trong, 1	m — 1	medium, w — weak, vw — very weak	

5.3. Fumarate dianion and fumaric acid vibrations

The 2APF-F crystal consists of both dianionic and neutral molecule of fumaric acid. C-H stretching vibrations are observed in the region $3102-3060 \text{ cm}^{-1}$. The CH stretching vibrations in the calculated spectrum are observed at 3073, 3069, 3058 and 3054 cm^{-1} . In the experimental IR and Raman spectra this band occurs at 3055 and 3056 cm⁻¹ with medium and strong intensity respectively. The C=C stretching vibrations are observed in the region 1645–1530 cm⁻¹. The stretching C=C vibrations are seen at 1638 cm⁻¹ for IR and 1636 cm⁻¹ for the Raman spectrum. Theoretically this vibration is calculated at 1629 $\rm cm^{-1}$ with strong intensity. The band at 1162 cm^{-1} with medium intensity in the Raman is assigned to CH in plane bending vibrations. The corresponding IR counterpart lies at 1172 cm^{-1} with strong intensity. Theoretically this peak is calculated at 1186 cm⁻¹. The band at 1411 cm⁻¹ in the theoretical spectrum can be assign to H–C bending vibration. The theoretically calculated OH stretching mode for free

(not bonding) carboxylic group is at 3609 cm^{-1} . The experimental value for this mode is at 2600 cm^{-1} in IR spectrum and not observed in the Raman spectrum. The stretching C=O band is observed in IR and the Raman spectra at 1700 cm^{-1} with their calculated values at 1728and 1708 cm^{-1} , respectively. The bands corresponding to C–O stretching mode appear at 1368 cm^{-1} in IR spectrum and 1337 $\rm cm^{-1}$ (very strong) for theoretical Raman spectra. The C–O bending bands are observed at IR and Raman spectra at 853 cm^{-1} . Calculated wavenumber of this vibration is at 882 cm^{-1} . The Raman band at 558 cm^{-1} with the calculated value at 581 cm^{-1} comes from out of plane bending vibration of OH group. The asymmetric and symmetric stretching modes of COO⁻ group are respectively observed at 1492 and 1382 $\rm cm^{-1}$. Their calculated counterparts are at 1502 (asymmetric) and 1487 cm^{-1} (symmetric). The bending modes of COO⁻ group are not observed in experimental spectra, but are visible on calculated spectrum at 708, 591, and 407 cm^{-1} .

5.4. 2-aminopyridine vibrations

Vibrations of 2-aminopyridine cation can be divided into vibrations of NH₂ group, NH stretching and bending vibrations and vibrations of the aromatic ring. Both amino groups are involved in creation of hydrogen bonds with fumarate dianion. The NH₂ groups in the aminopyridine are classified to asymmetric stretching, symmetric stretching, in-plane and out-of plane bending mode of vibrations. The calculated frequencies of NH₂ stretching (respectively asymmetrical and symmetrical) vibrations are lying at 3532 and 2860 cm^{-1} . The band observed at 1643 cm^{-1} in theoretical IR spectra is assigned to NH₂ in-plane bending vibration and in the experimental spectrum this peak is observed at 1550 cm^{-1} with strong intensity. The NH₂ in plane rocking modes are observed at 430 cm^{-1} in IR and Raman spectra, and calculated at 419 $\rm cm^{-1}.$ The wagging $\rm NH_2$ bands are observed at 733 cm^{-1} in IR spectra, at 752 cm^{-1} in calculated spectra and in the Raman spectra are not observed. Stretching vibration of NH group is observed at 1900 $\rm cm^{-1}$ and because of N1–H5...O3 hydrogen bond the band is broad. The band corresponding to C–N stretching vibrations is calculated at 1695 cm^{-1} . Experimentally this peak occurs at 1675 cm^{-1} in the IR spectra and at 1660 cm^{-1} in the Raman spectra. The bands from C–N bending vibrations are observed at 550 cm⁻¹ (in plane bending) and at 374 cm⁻¹ (out of plane). The ring out of plane C–N vibrations can be seen at 392 cm^{-1} in IR spectrum and at 396 cm^{-1} in Raman spectrum. Calculated counterparts are at 511 and 393 cm^{-1} .

5.5. H-bonds vibrations

In the title crystal are five hydrogen bonds of N-H...O, O-H...O and C-H...O type. The N-H...O types cover the range 2.77–2.94 Å, the O–H...O hydrogen bond is the strongest one in the crystal and the distance between donor and acceptor is equal to 2.61 Å. The weakest hydrogen bond in the crystal is C–H...O type (3.18 Å). The two broad bands from O–H and N–H stretching vibrations are observed in IR spectra in the range $3500-2000 \text{ cm}^{-1}$. In the optimized geometry are only two hydrogen bonds of N-H...O type. The band derived from O-H...O stretching vibration in the IR spectrum is at 2600 cm^{-1} and is not observed in the theoretical spectrum. The N-H...O stretching vibration occurs at 1900 cm^{-1} with strong intensity. Upon deuteration, these bands are moved to 1950 and about 1600 cm^{-1} , respectively. The N-H...O out of plane bending vibration occurs at 1190 cm^{-1} . The IR band at 691 cm^{-1} is assigned to O-H...O out of plane bending vibrations, and its counterpart at deuterated analogue spectrum is at 685 cm^{-1} .

5.6. Frontier molecular orbital analysis

Frontier molecular orbital (HOMO–LUMO) analysis has been done to determine the molecular reactivity and the ability of a molecule to absorb light. It also plays an important role in electrical, optical properties, UV-Vis spectra and chemical reactions [23–26]. Also, the HOMO-LUMO energy gap is used to determine molecular electrical transport properties [25]. The calculated HOMO-LUMO for 2APF-F by B3LYP/6-311G(d,p) basis set is shown in Fig. 6. It is seen from Fig. 6 that electrons for HOMO are delocalized mainly on the 2aminopyridinium ring and on the carboxylate group (this group is hydrogen bonded with cation). However for the LUMO electrons are delocalized on the whole fumaric acid molecule. For the LUMO+1 electrons are delocalized practically on the whole molecule of bis(2aminopyridinium) fumarate fumaric acid 1:1 and for the HOMO-1 electrons are delocalized on the anion and partly on the nitrogen of 2-aminopyridinium cation. Energy gap between HOMO and LUMO equals 3.53 eV which show that the charge transfer occurs in 2APF-F molecule [26]. The chemical reactivity descriptors of molecules such as chemical potential μ , electronegativity χ , chemical hardness η and softness S are defined as follows:

$$\begin{split} \eta &= \frac{(I-A)}{2}, \quad S = \frac{1}{2\eta}, \\ \chi &= \frac{(I+A)}{2}, \quad \mu = -\frac{(I+A)}{2}, \end{split}$$

where I and A are the ionization potential and electron affinity of the molecules, respectively. The ionization energy and electron affinity can be expressed through HOMO and LUMO energies as $I = -E_{\rm HOMO}$ and $A = -E_{\rm LUMO}$. It is widely known that chemical hardness and softness are useful properties to measure the molecular stability and reactivity. A soft molecule has a small HOMO–LUMO gap and is more reactive than hard molecule which has a bigger energy gap.



Fig. 6. Frontier orbital analysis of 2APF-F.

In order to study the chemical reactivity and stability of 2APF-F, the chemical hardness, softness, electronegativity and chemical potential have been calculated and the results are presented in Table VI. To investigate the

TABLE VI

The calculated frontier orbital energies, ionization potential, electron affinity, hardness, softness, electronegativity, chemical potential for 2APF-F.

	Gas ph	ase ($\varepsilon = 1$)	Water ($\varepsilon = 78.39$)		
	α	β	α	β	
$E_{\rm HOMO}$	-6.97	-6.97	-6.77	-6.77	
$E_{\rm LUMO}$	-3.44	-4.73	-2.95	-5.42	
Ι	6.97	6.97	6.77	6.77	
A	3.44	4.73	2.95	5.42	
η	1.76	1.11	1.91	0.67	
S	0.28	0.44	0.26	0.73	
χ	5.20	5.85	4.86	6.09	
μ	-5.20	-5.85	-4.86	-6.09	

solvent effect for the chemical reactivity descriptors based on B3LYP/6-311++G(d,p) model and PCM method, one kind of solvent is used — water ($\varepsilon = 78.39$).

According to Table VI, energy gap between HOMO and LUMO orbitals for the dissolved particle is bigger than in the gas phase and increases from 3.53 eV to 3.82 eV. The chemical hardness increase and the softness decrease in the solution phase. The molecule in the gas phase is more reactive than in solution phase.

5.7. Determination of molecular electrostatic potential

The possible sites for electrophilic and nucleophilic reactions as well as hydrogen bonding interactions [27, 28] are determined by the molecular electrostatic potential (MEP). The MEP is a plot of electrostatic potential surface, i.e. plot of electrostatic potential mapped on the constant electron density surface. To predict reactive sites for nucleophilic and electrophilic attack for 2APF-F the MEP at the B3LYP/6-311++G(d,p) optimized geometry was calculated. Figure 7 shows the 3D plot of



Fig. 7. Molecular electrostatic potential map of 2APF-F.

2APF-F molecule with uniform total energy distribution. The electrostatic potential of the molecule is in the range -7.951×10^{-2} (deep red) to $+7.951 \times 10^{-2}$ (deep blue) where blue color indicates the strongest attraction and red indicates the strongest repulsion. The MEP map

shows that the negative potential sites are on the oxygen atoms and positive potential sites are around hydrogen atoms from carboxylic group. These sites give information concerning the region from where the compound can have the intermolecular interaction.

5.8. NBO analysis

To investigate intermolecular interactions, the NBO analysis was carried out for the title compound. For each donor NBO(i) and acceptor (j), the stabilization energy $E^{(2)}$ associated to electron delocalization between donor and acceptor is estimated as

$$E^{(2)} = -q_i \frac{F_{ij}^2}{\varepsilon_i - \varepsilon_j},$$

where q_i is the donor orbital occupancy, ε_i , ε_j are diagonal elements (orbital energies) and F_{ij} is the off-diagonal NBO Fock matrix element. The results of second-order perturbation theory analysis are collected in Table VII.

TABLE VII

Second-order perturbation theory analysis of the Fock matrix in NBO, calculated at B3LYP/6-311++G(d,p).

Donor orb. i	Acceptor orb. j	$E^{(2)}$	$\varepsilon_j - \varepsilon_i$	F_{ij}
LP(1) O27	BD*(1) O52-H56	5.51	1.02	0.09
LP(2) O27	BD*(1) O52-H56	15.21	0.68	0.13
LP(3) O27	BD*(1) O52-H56	1.06	0.63	0.03
LP(1) O27	BD*(1) N13-H22	4.60	1.26	0.96
LP(2) O27	BD*(1) N13-H22	1.84	0.91	0.05
LP(3) O27	$BD^{*}(1) N13-H22$	0.10	0.86	0.01
LP (1) O28	BD*(1) N14-H23	1.02	1.36	0.04
LP(2) O28	BD*(1) N14-H23	2.54	0.94	0.06
LP (3) O28	BD*(1) N14-H23	0.43	0.93	0.02
LP (1) O28	BD*(1) N38-H50	0.93	1.24	0.04
LP(2) O28	BD*(1) N38-H50	1.09	0.82	0.03
LP(3) O28	BD*(1) N38-H50	1.94	0.81	0.04
LP (1) O51	BD*(1) C19-H21	1.20	1.23	0.04
LP(2) O51	BD*(1) C19-H21	0.49	0.80	0.02
$E^{(2)}$ — en	nergy of hyper	conju	gative	interac-
tions [kcal/m between dono	nol]; $\varepsilon_j - \varepsilon_i - \epsilon_i$ r and acceptor <i>i</i> as	energy nd j Ni	differenc BO orbit	e [a.u.] als; <i>F</i> _{ij}
— the Fock m	natrix element [a.u.	betwe	en i and	j NBO
orbitals.				

It is seen that the biggest contribution to the stabilization energy of the system is due to $O2^a - H2^a \dots O3$ hydrogen bond. The stabilization energy between lone electrons pair on the O27 oxygen atom of the carboxylate group and the antibonding orbital $\sigma(O52-H56)$ equals 21.78 kcal/mol [29, 30]. The second according to the bond strength is the N1-H5...O3 hydrogen bond with the stabilization energy equals 6.54 kcal/mol. The remaining two hydrogen bonds of N-H...O type are weaker, the interaction energy between lone pairs n(O28) and antibonding orbital $\sigma(N14-H23)$ is equal to 3.99 kcal/mol, while the stabilization energy for N2-H9...O4^b hydrogen bond equals 3.96 kcal/mol. As it could be expected, on the basis of crystallographic data, the weakest bond in the studied system is unconventional hydrogen bond of C–H...O type between π -electrons of 2-aminopyridinium ring and oxygen atom lone pair of neutral molecule of fumaric acid. The stabilization energy of this bond equals 1.69 kcal/mol and corresponds to weak hydrogen bond. Crystallographic data and the results of NBO calculations are in good agreement. It is worthwhile mentioned that the results of theoretical calculations could not reflect the current situation in real crystal as for simulations one can choose several neighboring molecules only which are additionally located at the vacuum. Therefore the effects originating from crystal packing phenomena, i.e. intermolecular interactions, are neglected.

5.9. NLO properties

It is well known that the importance of polarizability and hyperpolarizability of a molecular system is dependent on the electronic communication of two different parts of a molecule. Nonlinear activity of any materials provides the key functions from applications point of views for frequency shifting, optical modulation, optical switching etc. for developing technologies in the area of communication, optical processing and interconnection [31, 32]. The dipole moment μ , polarizability α and the first hyperpolarizability β were calculated with the level of B3LYP/6-311++G(d,p) basis set on the basis of the finite field approach. The complete equations for calculating the magnitude of total static dipole moment μ , the mean polarizability α_0 , the anisotropy of the polarizability $\Delta \alpha$ and mean first polarizability β_0 , using the x, y, z components are obtained from the Gaussian output as follows:

$$\mu_{\text{tot}} = \left(\mu_x^2 + \mu_y^2 + \mu_z^2\right)^{1/2}, \quad \alpha_{\text{tot}} = \frac{\alpha_x x + \alpha_y y + \alpha_z z}{3},$$
$$\beta_{\text{tot}} = \left(\left(\beta_{xxx} + \beta_{xyy} + \beta_{xzz}\right)^2 + \left(\beta_{yyy} + \beta_{yzz} + \beta_{yxx}\right)^2 + \left(\beta_{zzz} + \beta_{zxx} + \beta_{zyy}\right)^2\right)^{1/2}.$$

TABLE VIII

Calculated dipole moments — μ , polarizability — α and the first hyperpolarizability — β components, all [a.u.], for the title compound.

			-
μ_x	-4.84	β_{xxx}	1156.63
μ_y	-1.42	β_{xxy}	537.93
μ_z	0.70	β_{xyy}	144.33
$\mu_{ m tot}$	5.10	β_{yyy}	25.02
α_{xx}	294.44	β_{xxz}	-348.14
α_{xy}	8.33	β_{xyz}	-86.43
α_{yy}	180.54	β_{yyz}	-39.11
α_{xz}	25.27	β_{xzz}	-9.76
α_{yz}	-13.59	β_{yzz}	6.28
α_{zz}	172.14	β_{zzz}	-26.96
$\alpha_{\rm tot}$	215.71	$\beta_{ m tot}$	1470.65

The calculated dipole moment, the polarizability and first hyperpolarizability are listed in Table VIII. Since the values of the polarizability (α_{tot}) and hyperpolarizability (β_{tot}) of the Gaussian 03 output are reported in atomic units (a.u.), the calculated values have been converted into electrostatic units (esu) (α : 1 a.u. = 0.148×10^{-24} esu and β : 1 a.u. = 8.639×10^{-33} esu). The calculated values of electric dipole moment, polarizability and the first hyperpolarizability of 2APF-F are 5.1003 D, 31.9252 Å³ and 1.27×10^{-29} cm⁵ esu⁻¹. The large value of first hyperpolarizability, which is more than 16 times greater than urea (0.78×10^{-30} cm⁵ esu⁻¹) may be associated with the large number of π conjugated bonds and intramolecular hydrogen bonds [33].

5.10. Thermodynamic properties

On the basis of vibrational analysis and statistical thermodynamics, the standard thermodynamic functions: constant volume heat capacity C_v , entropy S, and enthalpy H were obtained at B3LYP/6-311++G(d,p) level and listed in Table IX. Table IX shows that the standard heat capacities, entropies, and enthalpies increase at any temperature from 200.00 to 500.00 K, because the intensities of molecular vibration increase with the increasing temperature.

TABLE IX

Thermodynamic properties at different temperatures at B3LYP/6-311++G(d,p).

T [K]	$C_v \ [cal/(mol \ K)]$	$S \ [\mathrm{cal}/(\mathrm{mol} \ \mathrm{K})]$	$H \; [\text{kcal/mol}]$
200	63.04	167.61	169.88
250	73.44	183.21	173.40
298.15	83.50	197.38	177.27
300	83.88	197.91	177.43
350	93.94	211.91	181.98
400	103.33	225.34	187.01
450	111.91	238.25	192.49
500	119.66	250.66	198.39

The correlations between these thermodynamic properties and temperatures T are as follows:

$C_{p,m}^0 = 13.596 + 0.268T - 10^{-4}T^2 \ (R^2 = 0.9999),$
$S_m^0 = 100.02 + 0.3636T - 10^{-4}T^2 \ (R^2 = 1),$
$H_m^0 = 160.44 + 0.279T - 10^{-4}T^2 \ (R^2 = 1).$

6. Conclusion

Optimized geometry of bis(2-aminopyridinium) fumarate — fumaric acid (1:1) [2APF-F] has been obtained. Comparison of the crystal structure and the theoretically calculated geometry show small differences in bond lengths and atomic angles values. In spite of the differences observed in the geometric parameters, the general agreement is good and the calculated results support the solid-state structure. Several infrared and Raman modes have been identified and assigned for the title crystal. The theoretical and observed frequencies have been compared and several stretching and deformation modes confirm the presence of intermolecular hydrogen bonding in the title crystal. The present work is, therefore, an attempt to present a critical review of the data on which infra-red spectral correlations are based indicating the classes of compounds which have been studied in each case the factors which can influence the frequencies or intensities of the characteristic bands. The TD-DFT calculations on the molecule provided deep insight into their electronic structure and properties. The HOMO-LUMO energy gap supports the charge transfer interaction within the molecule. NBO charges clearly show that the hydrogen atoms which are involved in N-H...O bonds have a positive charge compared with other hydrogen atom in the molecule. The positive and negative potential sites in the molecular electrostatic potential surface confirm the existence of N-H...O, O-H...O and N–H...N intermolecular interactions in the solid state. The large value of first hyperpolarizability suggests that the studied molecule 2APF-F is a good candidate for higher order nonlinear optical applications.

References

- S. Goswami, A.K. Mahapatra, G.D. Nigam, K. Chinnakali, H. Kun Fun, I.A. Razak, *Acta Crystallogr. C* 55, 583 (1999).
- [2] A. Ballabh, D.R. Trivedi, P. Dastidar, E. Suresh, *Cryst. Eng. Commun.* 4, 135 (2002).
- [3] S. Dong, Y. Tao, X. Shen, Z. Pan, Acta Crystallogr. C 69, 896 (2013).
- [4] M. Solich, W. Krol, K. Skirmuntt, Pol. J. Chem. 67, 433 (2013).
- [5] F.C. Wang, J.G. Green, B.B. Gerhart, Anal. Chem. 68, 2477 (1996).
- [6] S. Eiem-Ong, M. Spohn, N.A. Kurtzman, S. Sabatini, *Kidney Int.* 48, 1542 (1995).
- [7] E. Castrano, P. Marzabal, F.J. Casado, A. Felipe, M. Pastor-Anglada, *Clin. Sci.* 92, 247 (1997).
- [8] K. Tsuchiya, T. Uchida, M. Kobayashi, H. Maeda, T. Konno, H. Yamanaka, *Urology* 55, 495 (2000).
- [9] M. Akao, K. Kuroda, *Chem. Pharmaceut. Bull.* 28, 2012 (1990).
- [10] E.M.S. Macoas, R. Fausto, J. Lundell, M. Pettersson, L. Khriachtchev, M. Rasanen, J. Phys. Chem. A 105, 3922 (2001).
- [11] S. Mohan, V. Ilangovan, Asian J. Chem. 3, 556 (1995).
- [12] G. Anandha Babu, R.P. Ramasamy, P. Ramasamy, *Mater. Chem. Phys.* 117, 326 (2009).
- [13] A. Novak, Struct. Bond. 18, 177 (1974).
- [14] A.S. Davydov, *Theory of Molecular Excitons*, McGraw-Hill, New York 1962.

- [15] Kuma Diffraction, KM4/CCD Users' Guide, Version 1.169, release April 2000, Wroclaw, Poland 2000.
- [16] G.M. Sheldrick, SHELXL, Program for Crystal Structure Refinement, University of Gottingen, Germany 1993.
- [17] G.M. Sheldrick, Acta Crystallogr. A 64, 112 (2008).
- H.B. Schlegel, [18] M.J. Frisch, G.W. Trucks, G.E. Suzerain, M.A. Robb, J.R. Cheeseman Jr., J.A. Montgomery, T. Vreven, K.N. Kudin, J.C. Burant, J.M. Millam, S.S. Iyengar, J. Tomasi, V. Barone, B. Mennucci, M. Cossi, G. Scalmani, N. Rega, G.A. Petersson, H. Nakatsuji, M. Hada, M. Ehara, Toyota, R. Fukuda, J. Hasegawa, M. Ishida, Κ. Nakajima, Y. Honda, O. Kitao, H. Nakai, Т M. Klene, X. Li, J.E. Knox, H.P. Hratchian, J.B. Cross, V. Bakken, C. Adamo, J. Jaramillo, Gomperts, R.E. Stratmann, О. R. Yazvev, A.J. Austin, R. Cammi, C. Pomelli, J.W. Ochterski, P.Y. Ayala, K. Morokuma, G.A. Voth, P. Salvador, J.J. Dannenberg, V.G. Zakrzewski, S. Dapprich, A.D. Daniels, M.C. S D.K. Malick, A.D. Rabuck, M.C. Strain, O. Farkas, K. Raghavachari, J.B. Foresman, J.V. Ortiz, Q. Cui, A.G. Baboul, S. Clifford, J. Cioslowski, B. Stefanov, G. Liu, A. Liashenko, P. Piskorz, I. Komaromi, R.L. Martin, D.J. Fox, T. Keith, M.A. Al-Laham, C.Y. Peng, A. Nanayakkara, M. Challacombe, P.M.W. Gill, B. Johnson, W. Chen, M.W. Wong, C. Gonzalez, J.A. Pople, Gaussian 09, Gaussian Inc., Wallingford (CT) 2003.
- [19] H. Tanak, Mol. Phys. 112, 1553 (2014).
- [20] M.H. Jamróz, Spectr. Acta A: Mol. Biomol. Spectr. 114, 220 (2013).
- [21] E.D. Glendening, A.E. Reed, J.E. Carpenter, F. Weinhold, NBO Version 3.1.
- [22] D. Michalska, R. Wysokiński, Chem. Phys. Lett. 403, 211 (2005).
- [23] J. Fleming, Frontier Orbitals and Organic Chemical Reactions, Wiley, London 1976.
- [24] T. Karakurt, M. Dincer, A. Cetin, M. Sekera, Spectrochim. Acta A 77, 189 (2010).
- [25] K. Fukui, *Science 218*, 747 (1982).
- [26] R.G. Pearson, J. Am. Chem. Soc. 107, 6801 (1985).
- [27] H. Tanak, M.K. Marchewka, M. Drozd, Spectrochim. Acta A 105, 156 (2013).
- [28] E. Scrocco, J. Tomasi, Adv. Quant. Chem. 11, 115 (1978).
- [29] P.A. Wood, F.H. Allen, E. Pidcock, *Cryst. Eng. Commun.* **11**, 1563 (2009).
- [30] G.R. Desiraju, Angew. Chem. Int. Ed. 50, 52 (2011).
- [31] C. Andraud, T. Brotin, C. Garcia, F. Pelle, P. Goldner, B. Bigot, A. Collet, J. Am. Chem. Soc. 116, 2094 (1994).
- [32] V.M. Geskin, C. Lambert, J.L. Brédas, J. Am. Chem. Soc. 125, 15651 (2003).
- [33] A.B. Ahmed, H. Feki, Y. Abid, C. Minot, Spectrochim. Acta A 75, 1315 (2010).