Theoretical and Experimental Analysis of Drying Various Geometrical Forms of Red Pepper

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In this study, a counter flow convection-type dryer was designed and manufactured. During experiments, four different geometrical forms of pepper specimens were dried in a complete (unsliced), perforated, crosscut, and longitudinally sliced forms. For each type of red pepper specimen, the experiments have been conducted at air velocity level of 0.5 m/s, relative humidity of 10–15%, and temperature of 55–60°C. The theoretical mathematical model of drying process was developed, considering the pepper’s bottom surface to be isolated. The drying curves of experimental results are compared to ones obtained from the theoretical analyses. The comparison showed that experimental results are consistent with the theoretical model. The best results, considering the drying duration, are collected from the specimens sliced longitudinally, which were followed by the crosscut specimens, perforated and unsliced-complete specimens, respectively.

1. Introduction

Being an industrial process, drying is commonly used for drying of products in chemistry, textile, ceramic, construction, timber, pepper and food sectors. The energy used in these sectors for drying has a significant share in total energy consumption. This rate reaches 6% in chemistry, 5% in textile, 11% in ceramic and construction, 11% in timber, 12% in food and 33% in paper sectors. Drying is one of the most significant methods used in preserving food products. Dried products can be sent to be further processed or they can be put on market. To preserve food products for a long time without decomposition, dried products can be sterilized. Drying can be used to obtain some products out of solutions and to reduce the mass of carried materials. In their study, performed drying in regular and irregular pepper stacks at constant temperatures of 50, 60, 70 and 80°C, in a tunnel-type dryer with air speed of 2 m/s [3]. Quericci and Nebra dealt in their study with drying kinetics of banana theoretically and experimentally in different drying air conditions. According to constant diffusion coefficient assumption, they determined the humidity content experimentally, during the drying process of banana. The results obtained by taking into consideration the mass flow occurring during banana’s shrinkage and transportation on its surface, showed features highly similar with other models. Diffusion and transportation coefficients were obtained by implementing experimental data. Numerical results and experimental results were compared and the most appropriate transportation limit conditions were obtained using a constant diffusion coefficient [4]. Dinçer and Dost researched humidity and heat conduction performances and humidity transfer parameters of properly cut timber, which is put to drying, Biot coefficient in the ranges of 0 < Bi < 100 and Bi > 100 [5] were obtained. In their research, Ertekin and Sultanoglu determined humidity sorption isotherms of green and red pepper at temperatures of 30, 45 and 60°C and relative humidity values in the range of 10% to 90%. With nonlinear regression analysis, the acquired experiment results were compared with other solution models [6]. Dinçer theoretically calculated humidity diffusion and humidity conduction coefficients for plane and cylindrical structures for reference range 0 < Bi < 100 of Biot coefficient, which is the one that is used most in the practice, in his study entitled “modeling of humidity conduction in drying of solid materials”. By comparing this theoretical study with experimental studies made by Akiyama for cylindrical structures and by Lewicki for plane structures (flat cut onion wedges), he found the correlation number \( r^2 > 0.99 \) between drying time and non-dimensional humidity content. Besides, he found Biot number 3.73 for flat cut onion and 0.035 for cylindrical structured starch powder. He calculated diffusion coefficients \( 5.45 \times 10^{-10} \text{ m}^2/\text{s} \) and \( 3.04 \times 10^{-7} \text{ m}^2/\text{s} \) respectively [7]. Simal et al. developed mathematical model for heat distribution during drying in cylindrical structures. Broccoli was cut cylindrically at 0.0070 ± 0.0014 m calibre and 0.020 m long. Then samples were kept in NaOH solution for 15 seconds at temperature of 100°C. They performed drying process in a hot air dryer, with a drying temperature between 50 and 90°C, and with 3 kg/m³ air mass flow rate. Drying temperature was attempted to stabilize with an automatic thermostat. Experiments were conducted at air

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velocity of as 2.7 m/s and drying temperature of 50, 60, 70, 80 and 90 °C. By taking shrinkage into consideration during drying, a mathematical model was developed according to Fick’s 2nd law. Runge-Kutta-Merson method was used for solution of the problem. Effective diffusion coefficient was determined as a function of humidity and temperature [8]. Pangavhane et al. conducted experiments with Thompson seedless raisin in a fixed-type commercial dryer with air velocity of 0.25, 0.50, 0.75 and 1.0 m/s, temperature of 50, 60, 70 and 80 °C, and relative humidity of 13%, 18% and 23%. They performed weighing measurement at every half an hour until the humidity content in raisin was 17%. As a result of experimental and theoretical studies, drying kinetics of thin shelled seedless Thompson raisin was solved with Page equality. Experimental and theoretical results showed similar values. It was observed that abrupt changes occur in the structure of raisin above drying temperature of 70 °C and its shell has shriveled and cracked. They stated that the most appropriate drying temperature is between 50–70 °C [9]. Doymaz and Palal conducted a theoretical and experimental study of the drying kinetics of red peppers under different pretreatment and air drying conditions [10]. Scala and Crapiste simulated the process of drying of individual pieces of red pepper under constant external conditions and, to predict changes in some nutritional and organoleptic attributes of the product. Water sorption isotherms of red pepper were determined in the range 20–50 °C and represented by two different sorption equations. Drying kinetics was described by a diffusive model, the effective moisture diffusivity ranging from 5.01 to 8.32 × 10⁻¹⁰ m²/s with an activation energy of 23.35 kJ/mol were obtained. Degradation kinetics for ascorbic acid and total carotenoids were measured in the range 50–70 °C and modeled as the first-order reactions [11]. Faustino at al. studied the drying of green peppers, in terms of drying kinetics evaluated at 30 °C, 40 °C, 50 °C, 60 °C and 70 °C, and fitted experimental data to different empirical kinetic models from literature. This kinetic study was then complemented with the modeling in terms of Fick’s diffusion equation [12]. Vega et al. studied and modeled the drying kinetics of the red bell pepper at different temperatures (50, 60, 70 and 80 °C), using air velocity of 2.5 m/s. They observed only the falling rate period during the experiment. Effective moisture diffusivity was estimated to be between 3.2 × 10⁻⁹ and 11.2 × 10⁻⁹ m²s⁻¹ within the studied temperature range [13].

2. Materials and methods

2.1 Solar supported counter-flow convection dryer

Thermal input, required for the drying, was provided from two heat sources, a reflective sun-light collector and an additional sensitive resistance heater. When the external air is brought into the system via a duct, its temperature is being increased by the resistive heater. Hot air is directed onto the conveyor belt by a blowing fan. After passing over the drying peppers, having opposite flow direction, drying air is discharged at heat transformer, in which heat storage is performed in a PCM (Phase Change Material) with the help of air suction fan. In this way, heat recovery is achieved by discharging the the used hot air over PCM and over the intake air. Device’s band speed can be changed between 0 and 0.05 m/s with the inverter (speed control device), connected to motor-reductor group which is connected with band using a belt-pulley mechanism. Thus, the time between the entry and the exit of a spot on the band can be reduced down to 1.27 minutes. In this way, product drying time can be changed with the change of speeds at a stable tunnel length, thus the opportunity to dry different products is created. Supply and exhaust fans were employed in the experimental setup. Supply fan is of a radial type. Since it has a rotational speed control facility it is possible to send the air into the collector with varying speeds. Temperature control in the collector was performed by a PC connected PLC.

Drying different products with the aid of computer program is achieved with additional heater, at different temperatures, according to entered drying values. The designed and manufactured solar supported counter flow-convection type dryer is presented in Fig. 1. Front view of counter flow-convection type dryer is shown in Fig 1a. Side view of counter flow-convection type dryer is shown in Fig 1b. Product and air flow diagram of counter flow-convection type dryer is shown in Fig. 1c.
total mass of 100 g was cut and turned into samples with a mass of roughly 3 g. They were weighted on scales with 250 g capacity and 1/1000 sensitivity. Differences of the change rate of amount of dry material and moisture appeared, depending on the type of pepper, different ways of growing, measurement errors, and seed loss in pepper, which was cut in different shapes and depending on the air speed during the measurement. The amount of dry material was found to be 18%, and that of moisture was 82%. In order to determine the humidity of the air, temperatures of a wet and a dry thermometer were measured. Samples of different geometrical shapes prepared for drying are presented in Fig. 2. Unsliced-complete red pepper is shown in Fig. 2a. Perforated red pepper is shown in Fig. 2b. Crosscut red pepper is shown in Fig. 2c. Longitudinally red pepper sliced lengthwise is shown in Fig. 2d.

![Fig. 2. Red pepper of different geometrical forms prepared for drying, (a) unsliced-complete red pepper, (b) perforated red pepper, (c) crosscut red pepper (d) longitudinally sliced red pepper.](image)

### 2.3. Mathematical model

According to Fick’s 2nd Law, for single dimension of Cartesian coordinate system, humidity loss that occurs in pepper stacks of thickness along z-axis can be written as follows:

$$\frac{\partial X_f}{\partial t} = D \frac{\partial^2 X_f}{\partial z^2},$$  \hspace{1cm} (1)

where \(D\) (m/s²) is the diffusion coefficient, \(t\) (s) is time and \(z\) (m) is the change of pepper stack height. For boundary conditions it is assumed that the infinite plate of thickness \(2L\), and initial temperature \(T_0\) is suddenly brought into contact with a fluid with temperature \(T_{\infty}\). With such boundary conditions, this equation can be solved by thinking of it as a mass transfer equivalent of heat transmission’s process in a transient state [14]. If \(X_{\infty}\) is defined and written as \(X = X_f - X_{\infty}\), based on the humidity of the air, we obtain

$$\frac{\partial X}{\partial t} = D \frac{\partial^2 X}{\partial z^2}. \hspace{1cm} (2)$$

According to drying system presented in Fig. 3, the initial and the boundary conditions for system are:

\[ t = 0, \ 0 \leq z \leq b, \ X = \bar{X}_f = X_b - X_{\infty} \]

\[ t > 0, \ z = b - D \frac{\partial X}{\partial z} |_{z=b} = \ h' \ X |_{z=b} \]

\[ t > 0, \ z = 0 \frac{\partial X}{\partial z} |_{z=0} = 0, \]

where \( b \) (m) is thickness of pepper meat and \( h' \) (m/s) is mass transfer coefficient. Solution of (2) is considered as a product of two functions, one of which depends on coordinate \( z \) and the other depends on time \( t \).

Using the definition of Fourier number \( F_{om} = \frac{Dt}{b^2} \), the time-dependent solution is obtained as

$$\bar{X} = 2 \sum_{n=0}^{\infty} \sin(\lambda_n b) \left[ \sin(\lambda_n b + \sin(\lambda_n b) \cos(\lambda_n b)) \right. \times \cos \left( \lambda_n z \right) e^{-\lambda_n b z} F_{om}.$$  \hspace{1cm} (3)

As a result of the numerical calculations, Biot number \( (Bi = \frac{h' b}{\lambda}) \) is found to be 112309 for all uncut peppers. For other shapes of red pepper samples, since these values are practically \( Bi_m > 100 \), it can be taken as \( Bi_m \rightarrow \infty \) [15]. By using relative equations with Biot number, coefficients of Eq. 3 are found. By inserting these coefficients into general solution, if \( \bar{X} = X_f - X_{\infty} \) and \( F_{om} \) transformations are written in their place in equation, if a solution is conducted for 1st term along \( z \) axis in pepper stacks of \( b \) thickness, equation (4) that shows the humidity loss \( (X_f) \), occurred in red pepper stacks is acquired.

$$\frac{X_f - X_{\infty}}{X_b - X_{\infty}} = \left[ \cos \left( \frac{\pi}{2b} \right) \exp \left( - \frac{\pi^2}{4b^2} \right) \right]. \hspace{1cm} (4)$$

### 3. Results and discussion

The weight loss in pepper samples of different geometrical forms is calculated with measurements performed every 2 hours at a scales with 1/1000 sensitivity. Results of experimental studies: air speed 0.5 m/s, relevant humidity rate 10–15% and drying temperature are calculated as 55–60 °C. Weight loss of red peppers in different geometrical shapes, obtained as a result of experiment is presented in Table II and the humidity loss (%) is presented in Table II and Fig. 4. 82% of water (humidity) in 500 g sample were reduced to 4% in longitudinally sliced samples, to 6% in crosscut samples, to 7.5% in perforated samples and to 8% in unsliced-complete samples after 14 hours of drying.
Measurement of mass (g) of red peppers with different geometry, as function of time.

<table>
<thead>
<tr>
<th>Drying time, [h]</th>
<th>0</th>
<th>2</th>
<th>4</th>
<th>6</th>
<th>8</th>
<th>10</th>
<th>12</th>
<th>14</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unsliced</td>
<td>500</td>
<td>375</td>
<td>264.7</td>
<td>152.5</td>
<td>118.4</td>
<td>109.5</td>
<td>101.1</td>
<td>97.8</td>
</tr>
<tr>
<td>Perforated</td>
<td>500</td>
<td>300</td>
<td>225</td>
<td>142.9</td>
<td>118.4</td>
<td>107</td>
<td>98.9</td>
<td>97.2</td>
</tr>
<tr>
<td>Crosscut</td>
<td>500</td>
<td>300</td>
<td>176.5</td>
<td>121.6</td>
<td>111.1</td>
<td>104.5</td>
<td>97.8</td>
<td>95.7</td>
</tr>
<tr>
<td>Longitud. sliced</td>
<td>500</td>
<td>272.7</td>
<td>157.9</td>
<td>115.4</td>
<td>107.1</td>
<td>102.2</td>
<td>95.7</td>
<td>93.7</td>
</tr>
</tbody>
</table>

Humidity (%) of red peppers of different geometry as a function of time.

<table>
<thead>
<tr>
<th>Drying time, [h]</th>
<th>0</th>
<th>2</th>
<th>4</th>
<th>6</th>
<th>8</th>
<th>10</th>
<th>12</th>
<th>14</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unsliced-complete</td>
<td>0.82</td>
<td>0.76</td>
<td>0.66</td>
<td>0.41</td>
<td>0.24</td>
<td>0.16</td>
<td>0.11</td>
<td>0.08</td>
</tr>
<tr>
<td>Perforated</td>
<td>0.82</td>
<td>0.75</td>
<td>0.60</td>
<td>0.37</td>
<td>0.24</td>
<td>0.14</td>
<td>0.09</td>
<td>0.0675</td>
</tr>
<tr>
<td>Crosscut</td>
<td>0.82</td>
<td>0.70</td>
<td>0.49</td>
<td>0.26</td>
<td>0.19</td>
<td>0.12</td>
<td>0.08</td>
<td>0.06</td>
</tr>
<tr>
<td>Longitud. sliced</td>
<td>0.82</td>
<td>0.67</td>
<td>0.43</td>
<td>0.22</td>
<td>0.16</td>
<td>0.10</td>
<td>0.06</td>
<td>0.04</td>
</tr>
</tbody>
</table>

Ash content (weight percentage).

<table>
<thead>
<tr>
<th>Samples</th>
<th>Amount [%]</th>
<th>Most wanted in TS 2419</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unsliced-complete</td>
<td>9.3</td>
<td>8.5</td>
</tr>
<tr>
<td>Perforated</td>
<td>7.9</td>
<td>8.5</td>
</tr>
<tr>
<td>Crosscut</td>
<td>7.7</td>
<td>8.5</td>
</tr>
<tr>
<td>Longitudinally sliced</td>
<td>7.7</td>
<td>8.5</td>
</tr>
</tbody>
</table>

However, since the membrane shell was torn in the crosscut and longitudinally sliced red peppers, heating occurred in a shorter period of time and humidity loss started immediately. Thus the humidity loss in samples is decreasing in following order: in longitudinally sliced, crosscut, perforated and unsliced-complete samples. The ash contents and colours of samples obtained after drying are presented in Table III and Table IV respectively.

4. Conclusions

In the opposite flow type dryer device which was designed and produced, by taking advantage of Fick’s 2nd law, mathematical model of time-dependent humidity loss, which occurs along z axis in a red pepper stack of width b is prepared. A comparison of the results, obtained in experiments performed by a weight loss method, and the theoretical results obtained as a result of mathematical modeling was carried out. It is determined that with the exception of the uncut red peppers, the theoretical and experimental results are highly similar and that
are in accordance with each other. It is found that the change difference between theoretical drying curve and experimental drying curve in all uncut red peppers is a little higher than in other samples, and that this is the result of the air gaps between the uncut pepper stacks.

Comparison of the drying periods of red pepper samples, which are dried in different geometrical shapes, shows that the shortest drying time was obtained in longitudinally cut samples, followed by the cross cut, perforated and whole red pepper samples. 82% water (humidity) ratio in 500 g sample was reduced to 4% in longitudinally cut samples, 6% in crosscut samples, 7.5% in perforated samples and 8% in uncut whole samples after 14 hours of drying. However, if the processing facilitation is considered, based on automation possibilities, it is suggested to crosscut red peppers in pepper drying processes.

References


