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# Comparative Study of Compressibility of $\text{Ni}_2\text{MnX}$ ( $X=\text{In, Sn, Sb}$ ) Heusler Alloys

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The present study is focused on the compressibility of  $\text{Ni}_2\text{MnX}$  ( $X = \text{In, Sn, Sb}$ ) Heusler alloys, which were investigated from the first principles. The study of the pressure effect on the magnetic properties of  $\text{Ni}_2\text{MnX}$  ( $X = \text{In, Sn, Sb}$ ) predicted the decrease in the total magnetic moment from ambient pressure to pressure above 20 GPa.

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## 1. Introduction

An increasing interest in the Heusler alloys has been motivated by the search of ferromagnetic materials suitable for application in spintronic devices [1] or for magnetic actuator [2]. An understanding of the mechanical behaviour of some materials is also important for their applications. *Ab initio* calculations provide a microscopic framework to study the cohesion and deformation behaviour of these systems. Effect of hydrostatic pressure on the Curie temperature ( $T_C$ ) for  $\text{Ni}_2\text{MnX}$  ( $X = \text{Al, Ga, In, Sn, Sb}$ ) has been experimentally studied in [3]. The change of magnetisation of  $\text{Ni}_{2-x}\text{Mn}_{1-x}\text{Ga}$  experimentally studied on pressure [4] is consistent with features of electron band structure of the alloy. The isothermal compressibility and the Mössbauer high-pressure experiments of  $\text{Ni}_2\text{MnSn}$  have been performed by Gavriliuk et. [5]. Moreover, increase in the experimental value of  $T_C$  with pressure in  $\text{Ni}_2\text{MnSn}$  [5] is well confirmed by *ab initio* calculations [6]. The present *ab initio* studies are addressed to cohesive properties of  $\text{Ni}_2\text{MnX}$  ( $X = \text{In, Sn, Sb}$ ) (equilibrium lattice constant, cohesive energy), the mechanical properties (bulk modulus, its derivative) and to pressure behaviour of magnetic moments.

## 2. Method of calculation

The ground state calculations were performed using the full-relativistic calculations in the full-potential nonorthogonal local-orbital minimum basis (FPLO)

scheme [7, 8] with exchange-correlation potential in the form from [9]. The studied alloys have cubic  $L2_1$  structure. The lattice contains four interpenetrating fcc sublattices at positions (0,0,0) for Mn,  $(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$ ,  $(\frac{3}{4}, \frac{3}{4}, \frac{3}{4})$  for Ni and  $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$  for X (X = In, Sn, Sb). Ni 4s, 4p, 3d states, Mn 4s, 4p, 3d states, In, Sn, Sb 5s, 5p, 4d states, were chosen as a minimum-basis set for the valence states. The Brillouin zone integrations were performed using the tetrahedron method and 732  $k$ -points used in its irreducible part.

### 3. Results and discussion

The performed calculations clearly favour the ferromagnetic ground state for  $\text{Ni}_2\text{MnX}$  (X = In, Sn, Sb). We have optimized the lattice parameters for studied series in  $L2_1$  structure and calculated their cohesive energies ( $E_{\text{coh}}$ ).  $E_{\text{coh}}$  is an energy required to separate components of a compound into neutral free atoms.  $E_{\text{coh}}$  of the compounds is calculated as the total energy difference between the elemental components and the compound at equilibrium lattice constant. The calculated values of the  $E_{\text{coh}}$  of the studied alloys are given together with the equilibrium lattice parameters in Table. We pointed out that the determination

TABLE

The theoretical equilibrium lattice parameters ( $a$ ) in [ $\text{\AA}$ ], cohesive energies ( $E_{\text{coh}}$ ) [Ry/f.u.], bulk modulus ( $B$ ) in [GPa], its derivatives ( $B'$ ) and magnetic moments ( $m$ ) in [ $\mu_{\text{B}}$ ] of  $\text{Ni}_2\text{MnX}$  (X = In, Sb, Sn)

$x$	$a$	$E_{\text{coh}}$	$B$ [GPa]	$B'$	$m$
$\text{Ni}_2\text{MnIn}$	5.96	2.7452	168.5	4.2	4.05
$\text{Ni}_2\text{MnSn}$	5.92	2.8233	168.5	2.9	3.86
$\text{Ni}_2\text{MnSb}$	6.0	2.8317	168.3	6.0	3.87

of lattice parameter from minimum of the total energy for  $\text{Ni}_2\text{MnX}$  (X = In, Sn, Sb) yields results that are systematically somewhat smaller than the experimental values [10]. *Ab initio* calculations are strictly valid at absolute zero (T = 0 K) which should explain some observed differences between the theoretical results and experimental values of lattice parameter as well as magnetic moments [3, 10]. The bulk modulus expresses the material resistance to hydrostatic pressure. The total energy dependences on the cell volume for studied  $\text{Ni}_2\text{MnX}$  are fitted by the Murnaghan equation of state (EOS) [11] to obtain bulk modulus ( $B$ ) and its pressure derivative ( $B'$ ). Its values are summarised in Table. The obtained values of  $B$  for  $\text{Ni}_2\text{MnSn}$  and  $\text{Ni}_2\text{MnIn}$  are higher than achieved in other *ab initio* studies [2, 12]. This may reflect the fact that different first principles methods were used as well as fact that presented results were obtained on the assumption of spin-orbit

interaction. The pressure–volume relation for studied systems was calculated as the negative volume derivative of the total energy. The isothermal (at  $T = 0$  K) pressure–volume relationship is shown in Fig. 1. Figure 2 illustrates the change of

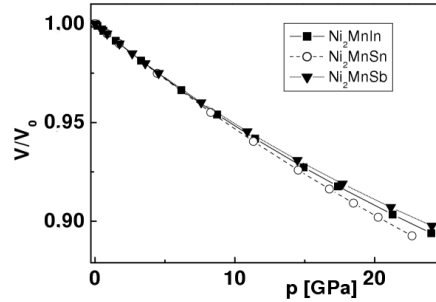


Fig. 1. The  $p$ - $V$  relation for  $\text{Ni}_2\text{MnX}$  ( $X = \text{In}, \text{Sn}, \text{Sb}$ ).

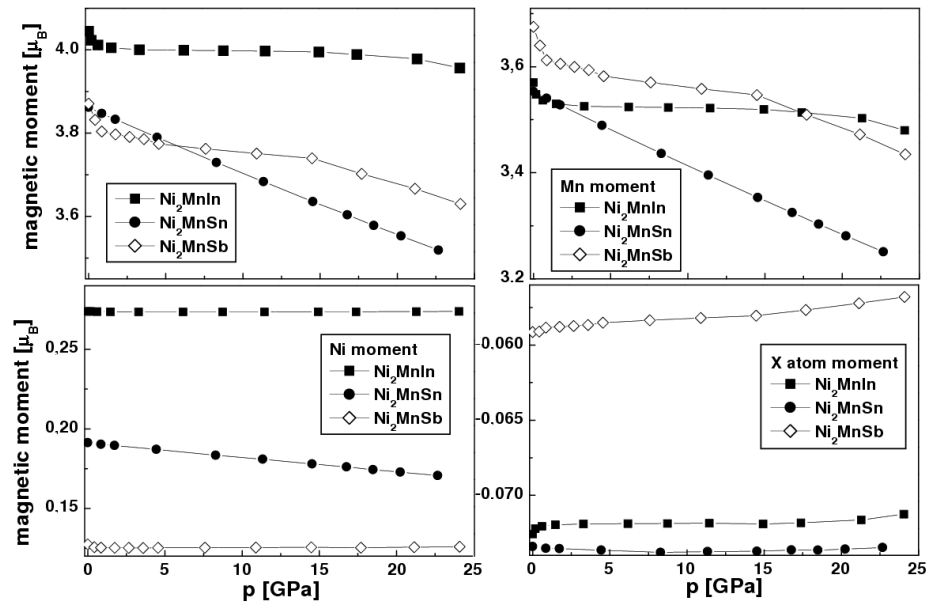


Fig. 2. The pressure dependence of the total and local magnetic moments in  $\text{Ni}_2\text{MnX}$  ( $X = \text{In}, \text{Sn}, \text{Sb}$ ).

the total and the local spin magnetic moments with pressure. The linear decrease in the total magnetic moment with pressure for  $\text{Ni}_2\text{MnSn}$  is in good agreement with previous calculation [6]. For  $\text{Ni}_2\text{MnIn}$  and  $\text{Ni}_2\text{MnSb}$  the response of the total moment to pressure is initially nonlinear and is connected with behaviour of Mn moment under pressure. The pressure leads to a slight shift of  $3d$  Mn peaks to

lower energy and to decrease in magnitude of these peaks. In the low pressure region the magnitude of  $3d$  Mn bonding peaks decreases faster for  $\text{Ni}_2\text{MnSb}$  than for  $\text{Ni}_2\text{MnIn}$ . In  $\text{Ni}_2\text{MnSb}$  it causes a decrease in majority density of states of Mn as well as very sharp decrease in Mn moment at low pressure below 2 GPa. For these both alloys Ni moment has practically the same value ( $0.274 \mu_B$  for  $\text{Ni}_2\text{MnIn}$  and  $0.127 \mu_B$  for  $\text{Ni}_2\text{MnSb}$ ) in whole studied pressure region. For  $\text{Ni}_2\text{MnSn}$  Ni moment changes from  $0.19 \mu_B$  at ambient pressure to  $0.17 \mu_B$  at 20 GPa. Although the value of Ni moment for  $\text{Ni}_2\text{MnSn}$  is less than in [6] the pressure behaviour of the moment is the same. The induced moment on X atoms is opposite to the Mn and Ni moment. Its value slightly increases with pressure for studied  $\text{Ni}_2\text{MnX}$ .

#### 4. Conclusions

Using the FPLO *ab initio* method we have determined bulk modulus, its derivatives, cohesive energies, and volume–pressure relation for series  $\text{Ni}_2\text{MnX}$ . The obtained bulk modulus of  $\text{Ni}_2\text{MnIn}$  and  $\text{Ni}_2\text{MnSn}$  is larger than in previous calculations. It may follow from the fact that spin–orbit interaction was included in total energy calculations. A good agreement of linear behaviour of the total magnetic moment of  $\text{Ni}_2\text{MnSn}$  is found with the available *ab initio* results. For  $\text{Ni}_2\text{MnIn}$  and  $\text{Ni}_2\text{MnSb}$  the presented study predicts nonlinear pressure–magnetization relation for pressure from 0 GPa to 15 GPa.

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